How does turbulence change approaching a rotor?

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Induction zone experiment at DTU Wind Energy E. Simley et al, J. Renewable Sustainable Energy, 8 013301 (2016)

Met mast 280°



Results for mean wind and turbulence



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Results for mean wind and turbulence



- Stagnation clear
- σ_u (and σ_w) almost constant

Results for mean wind and turbulence



- Stagnation clear
- σ_u (and σ_w) almost constant
- Not much statistics

Vorticity based methods E. Branlard, 2017



- To a first approximation, the presence of the wind turbine does not affect the turbulence spectrum significantly.
- Slight decrease of energy at high frequencies implying a slight decrease of turbine loads
- Further investigations necessary to conclude whether effect is systematic.

The Nørrekær Enge Experiment

A. Peña et al, Wind Energ. Sci. 2 (2017)





- Pulse five-beam lidar on nacelle (only central beam used here)
- Ten ranges (49, 72, 95, 109, 121, 142, 165, 188, 235, and 281 m)

Induction flow measured by lidar

Nørrekær Enge



Quasi-steady fluctuations (very low frequencies)

$$f(\xi, \boldsymbol{a}, U_{\infty}) \equiv \frac{U}{U_{\infty}} = 1 - \boldsymbol{a} \left(1 + \frac{2\xi}{\sqrt{1 + 4\xi^2}} \right)$$
(1)

A slow fluctuation in U_{∞}

$$\frac{S(x)}{S_{\infty}} = \left(\frac{\partial U}{\partial U_{\infty}}\right)^2 \tag{2}$$

where S(x) is the spectrum at a low frequency at the position x while S_{∞} is the upstream, undisturbed spectrum.

$$\frac{\partial U}{\partial U_{\infty}} = \frac{\partial f}{\partial U_{\infty}} U_{\infty} + f = f - \left(1 + \frac{2\xi}{\sqrt{1 + 4\xi^2}}\right) \frac{\partial a}{\partial U_{\infty}} U_{\infty}$$
(3)

Induction as a function of U_{∞}

from 10-minute beam-0 measurements



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Comparison with theory for low frequencies



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LES approach

- Simulations with and without a SQT93-2.3 turbine with identical ambient flow
- Turbine simulated as an actuator disk
- Turbulence generated by Mann model at 8, 11 and 13 m/s (shear free)



Snapshot of streamwise velocity with rotor



without rotor

Spectra at rotor center



Energy of lowest three frequencies (full lines) compared to quasi-steady model (dots)



- Above rated the change of energy approaching the rotor is well predicted by model
- Below rated LES shows less reduction then model

Conclusion

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- LES supports (partially) the findings
- Higher frequencies remains to be investigated and measured