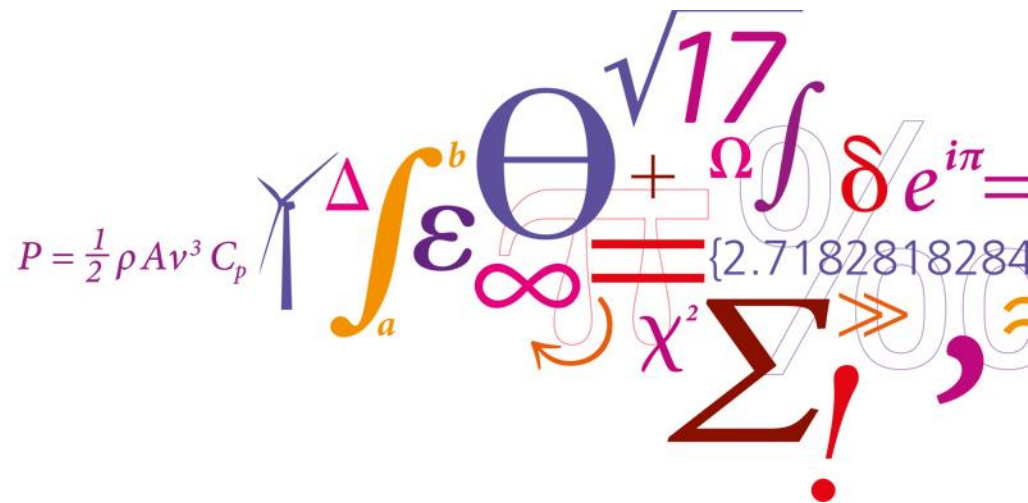
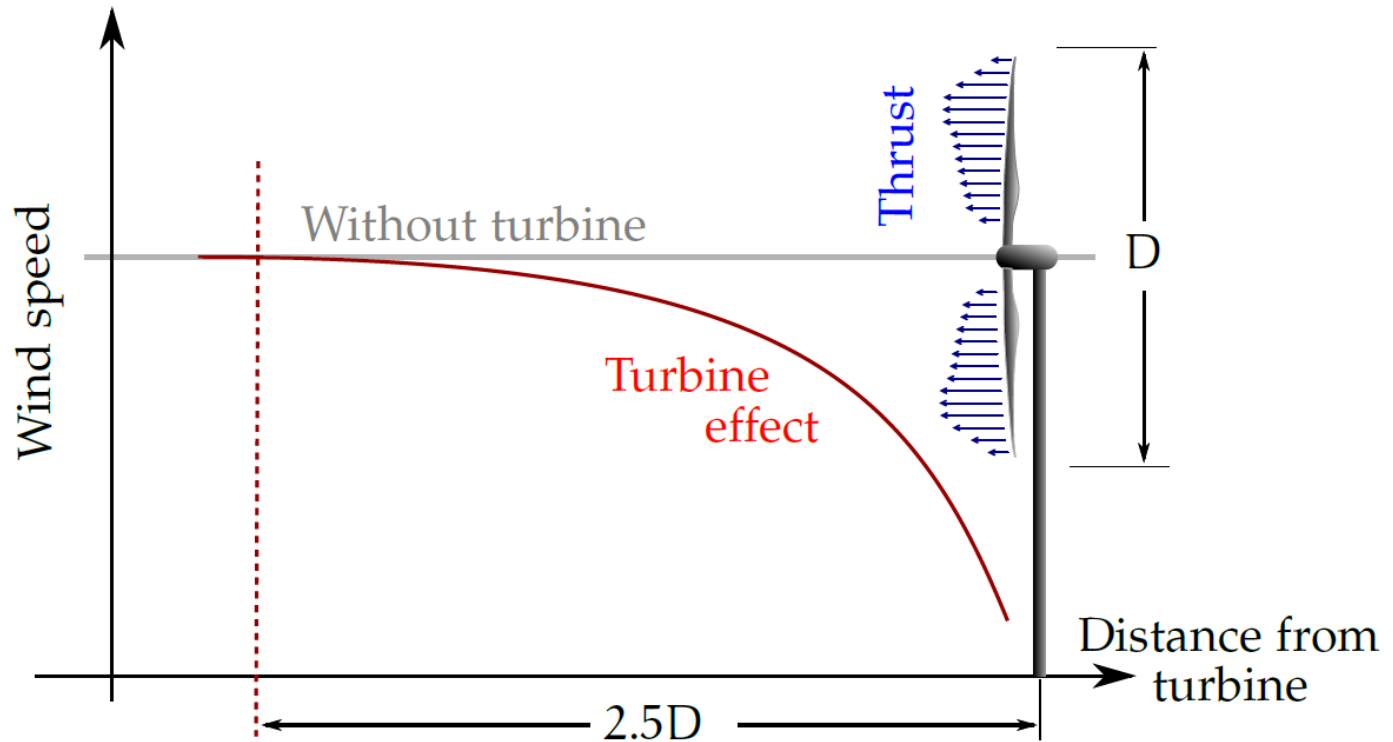


# Predicting free-stream wind speed in complex terrain with lidar measurements

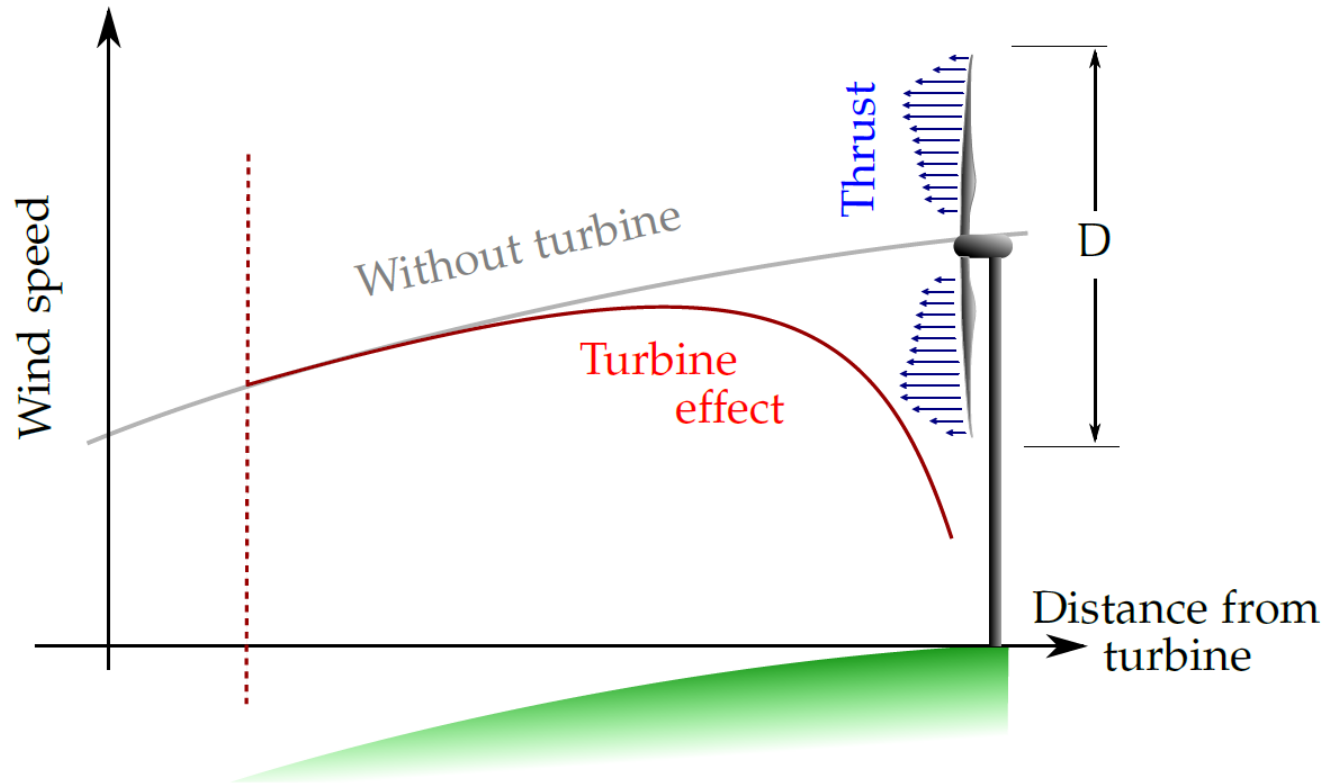
Alexander Meyer Forsting, Niels Troldborg,  
Andreas Bechmann



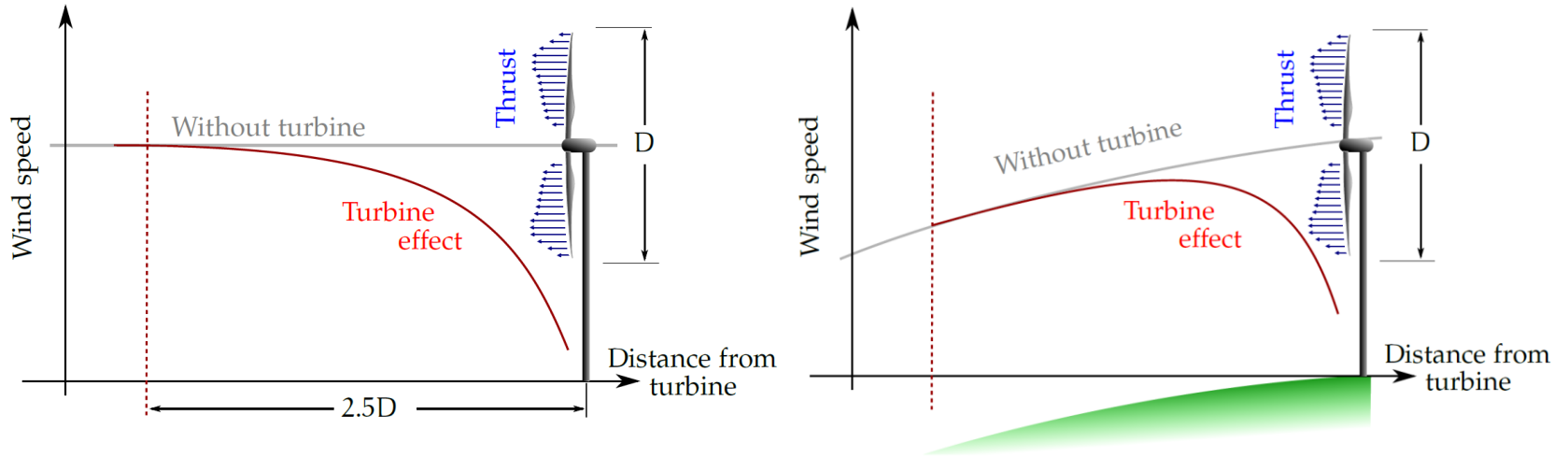
# The induction zone



# The induction zone in complex terrain



# Predict free-stream?

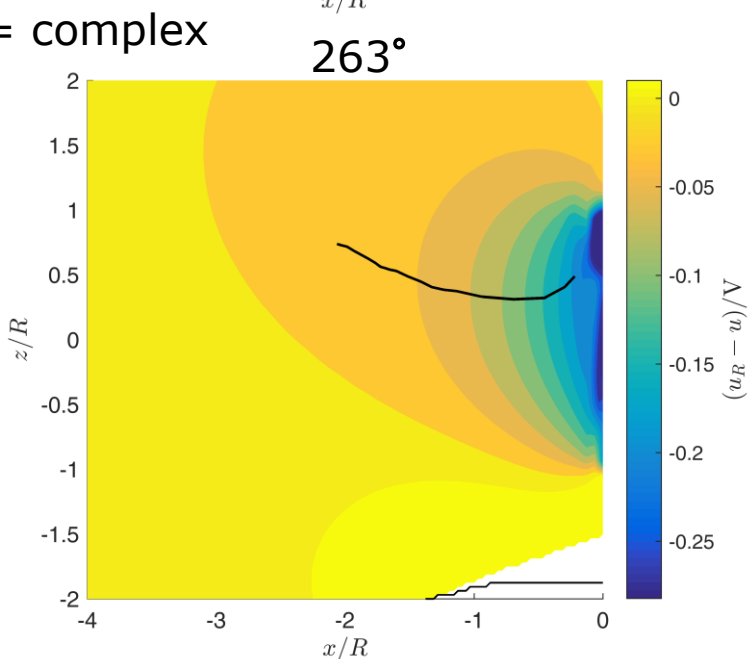
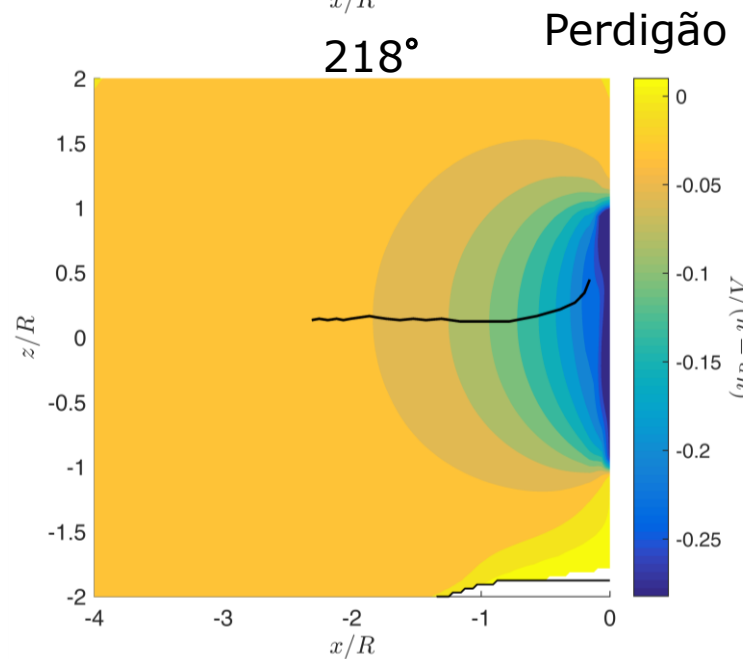
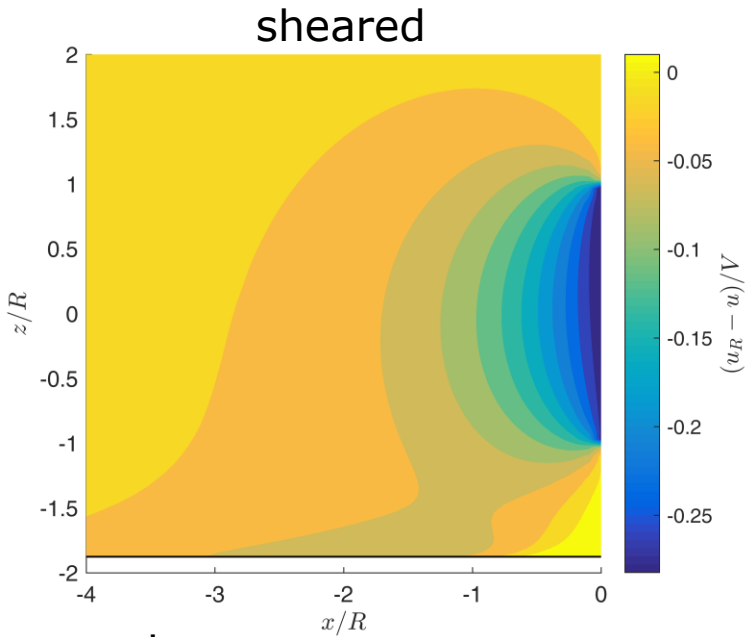
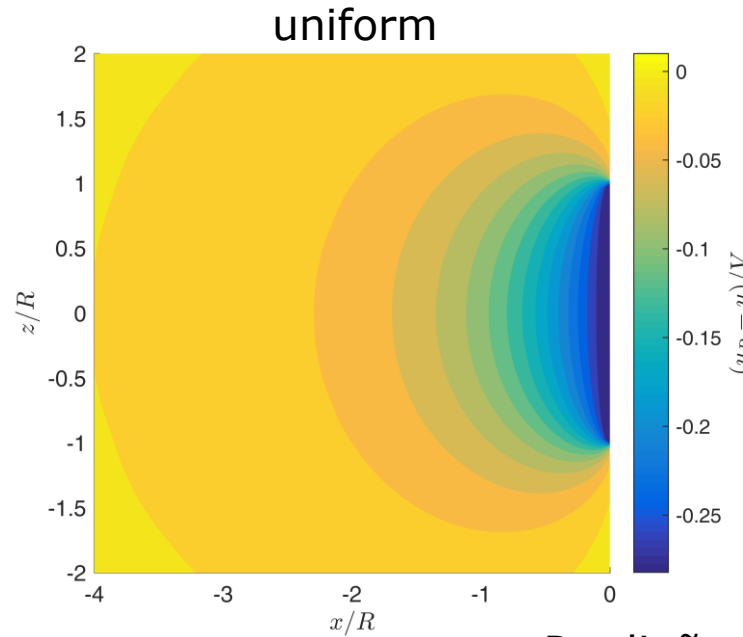


Universal induction zone



Same method to retrieve  $V_\infty$

# Universal ?

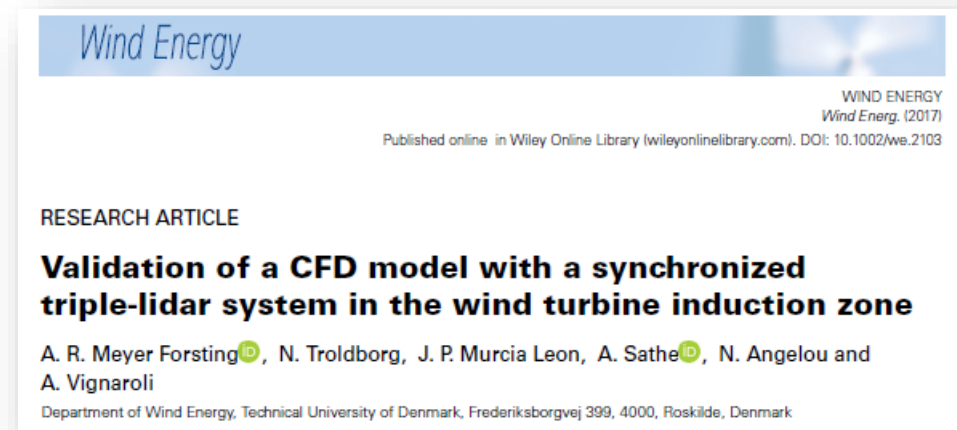


# Test universality

Parametric study with EllipSys3D



Use simple vortex model to predict induction zone



Wind Energy

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Wind Energ. (2017)  
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RESEARCH ARTICLE

**Validation of a CFD model with a synchronized triple-lidar system in the wind turbine induction zone**

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[www.wind-energ-sci.net/2/269/2017/](http://www.wind-energ-sci.net/2/269/2017/)  
doi:10.5194/wes-2-269-2017  
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## Wind field reconstruction from nacelle-mounted lidar short-range measurements

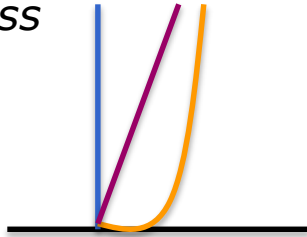
Antoine Borraccino<sup>1</sup>, David Schlipf<sup>2</sup>, Florian Haizmann<sup>2</sup>, and Rozenn Wagner<sup>1</sup>

<sup>1</sup>DTU Wind Energy, Roskilde, Denmark

<sup>2</sup>Stuttgart Wind Energy, University of Stuttgart, Stuttgart, Germany

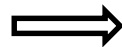
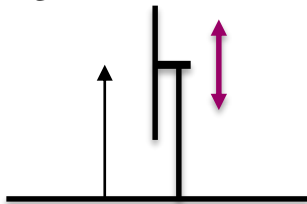
# Identify parameters influencing induction zone

*Roughness*



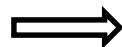
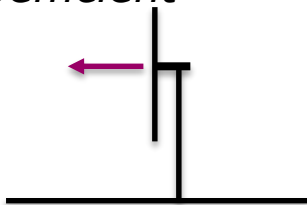
Log-law with **3** different  $z_0$   
0, 0.05m and 0.5m

*Hub Height*



**3** different  $h$   
0.7D, 1D, 1.5D

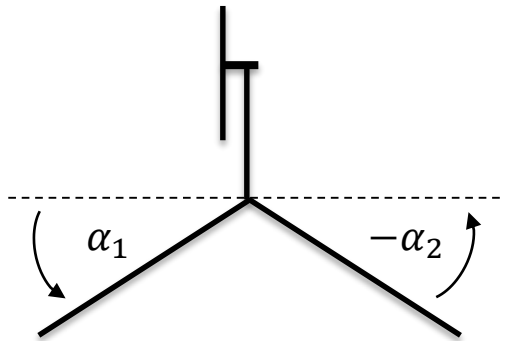
*Thrust coefficient*



**3** different  $C_T$   
0, 0.36, 0.89

# Identify parameters influencing induction zone

*Terrain*

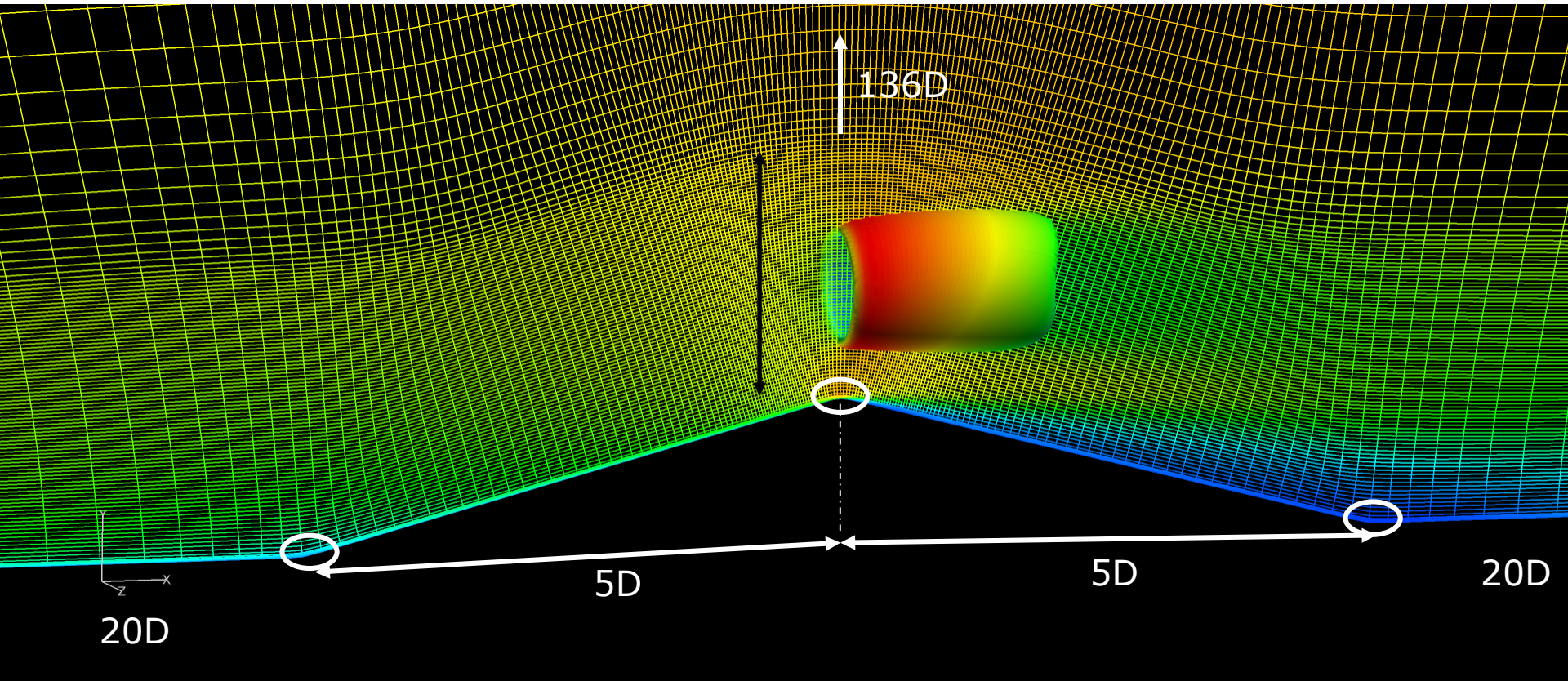


**7** different  $\alpha$ , **49** terrains  
-15:5:15 degrees

**1323** CFD simulations

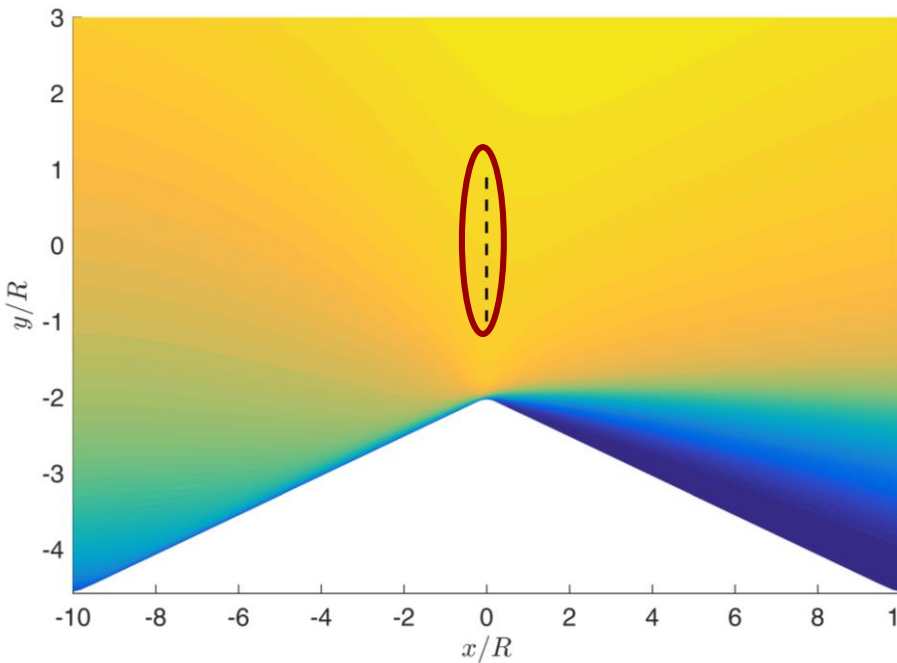


# Numerical approach

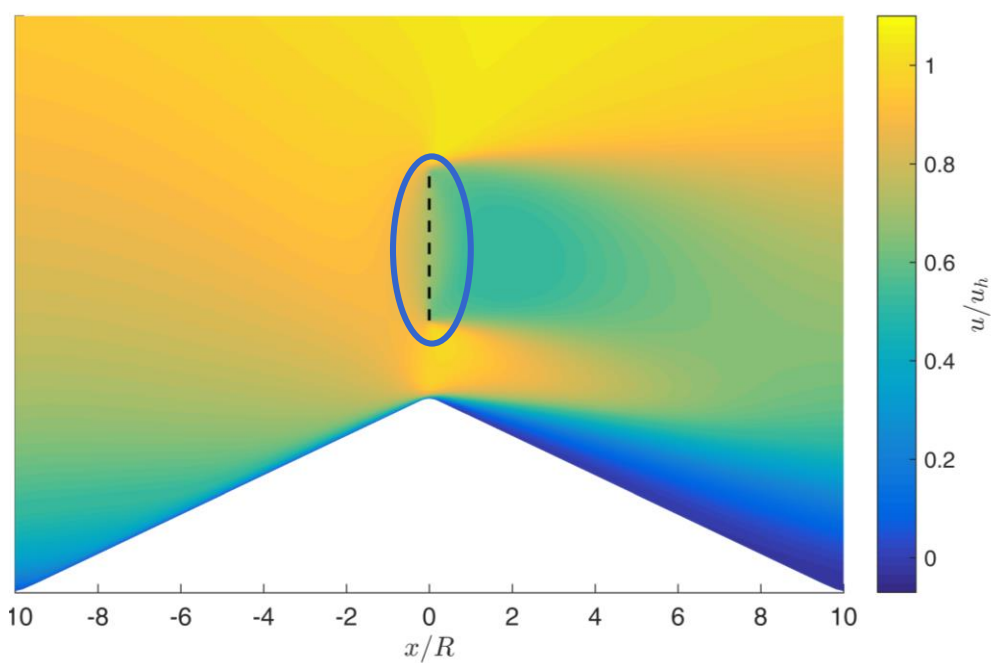


# Flow over hill

Free-stream reference



Turbine flow



$$F_{\{N, \Delta A\}} = \frac{1}{2} \rho_{\infty} V_{\{\infty, \Delta A\}}^2 C_T \Delta A$$

# Test simple model

Use simple induction zone model

$$\tilde{U}(\tilde{r}, \tilde{x}) = 1 - a(0, \tilde{x})f(\epsilon)$$

Longitudinal = vortex sheet

$$a(0, \tilde{x}) = a_0 \left( 1 + \frac{\tilde{x}}{\sqrt{1 + \tilde{x}^2}} \right)$$

$$a_0 = \frac{1}{2} (1 - \sqrt{1 - \gamma C_T})$$

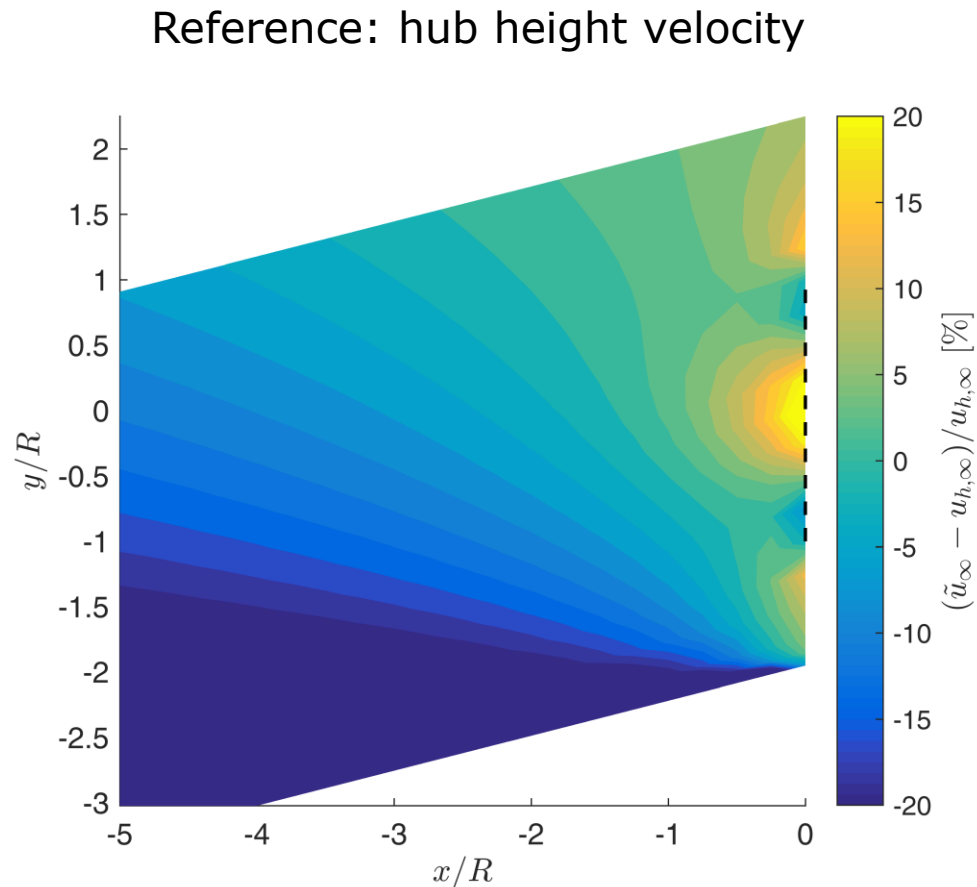
Radial variation

$$f(\epsilon) = \operatorname{sech}^\alpha(\beta\epsilon)$$

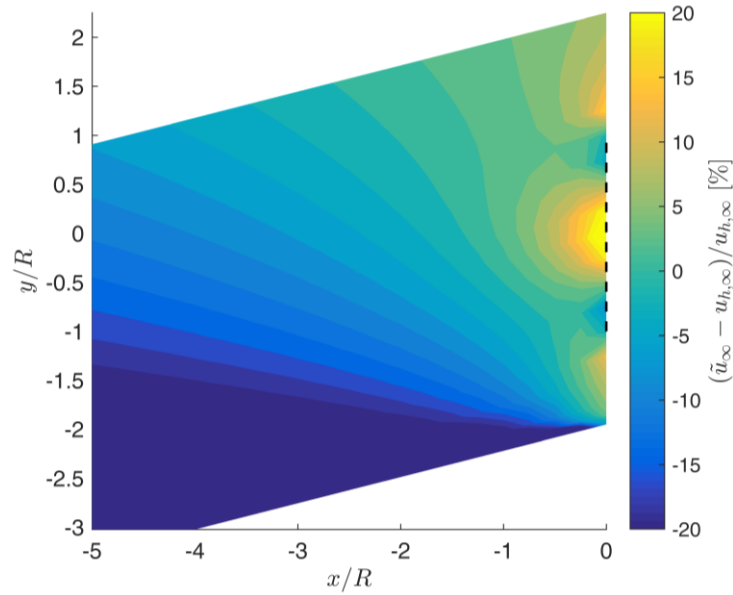
$$\tilde{U}(r, x) = \frac{U(r, x)}{U_\infty}, \quad \epsilon = \frac{r}{r_{1/2}(x)}, \quad \tilde{r}_{1/2}(x) = \frac{r_{1/2}(x)}{R}, \quad \tilde{r} = \frac{r}{R}, \quad \tilde{x} = \frac{x}{R}$$

# Model prediction error

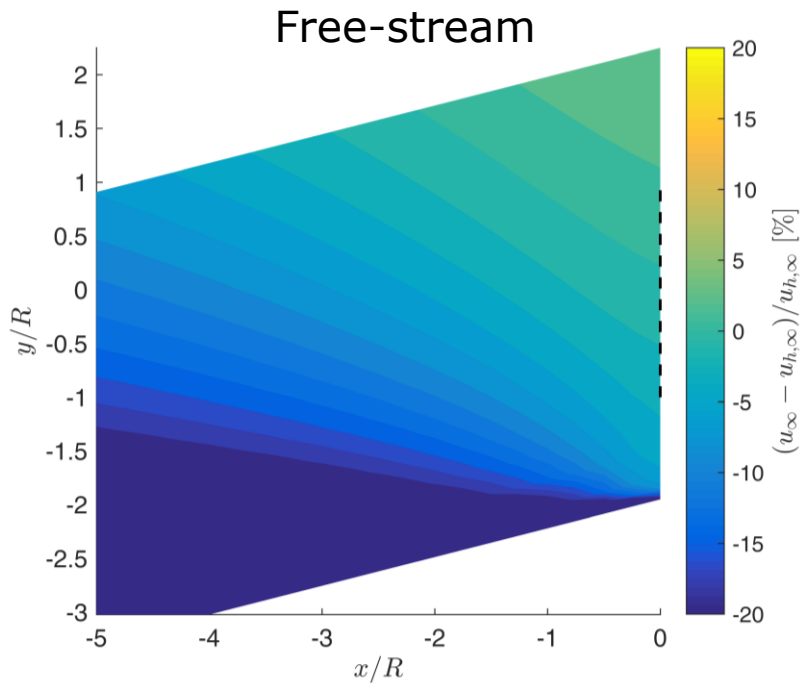
$\alpha_1 = 15 \text{ deg}$   
 $\alpha_2 = -15 \text{ deg}$   
 $z_0 = 0.5 \text{ m}$   
 $h = 1D$   
 $C_T = 0.89$



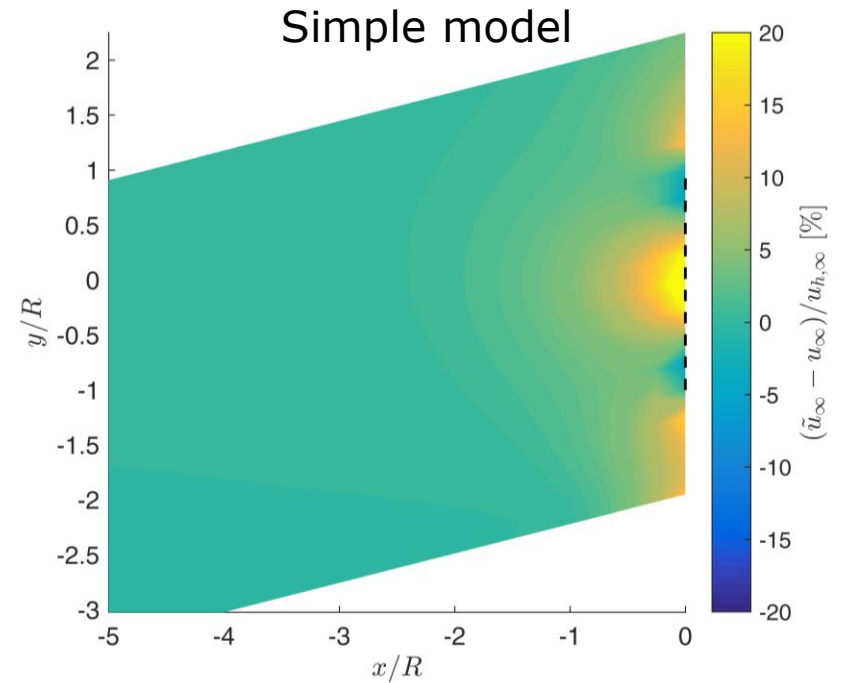
# Split error



=

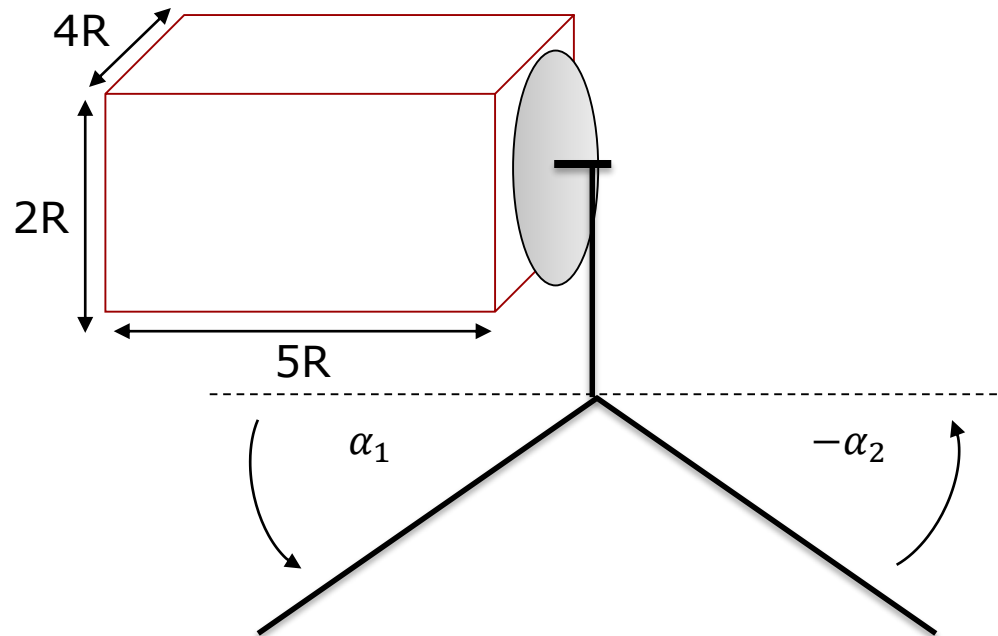


+



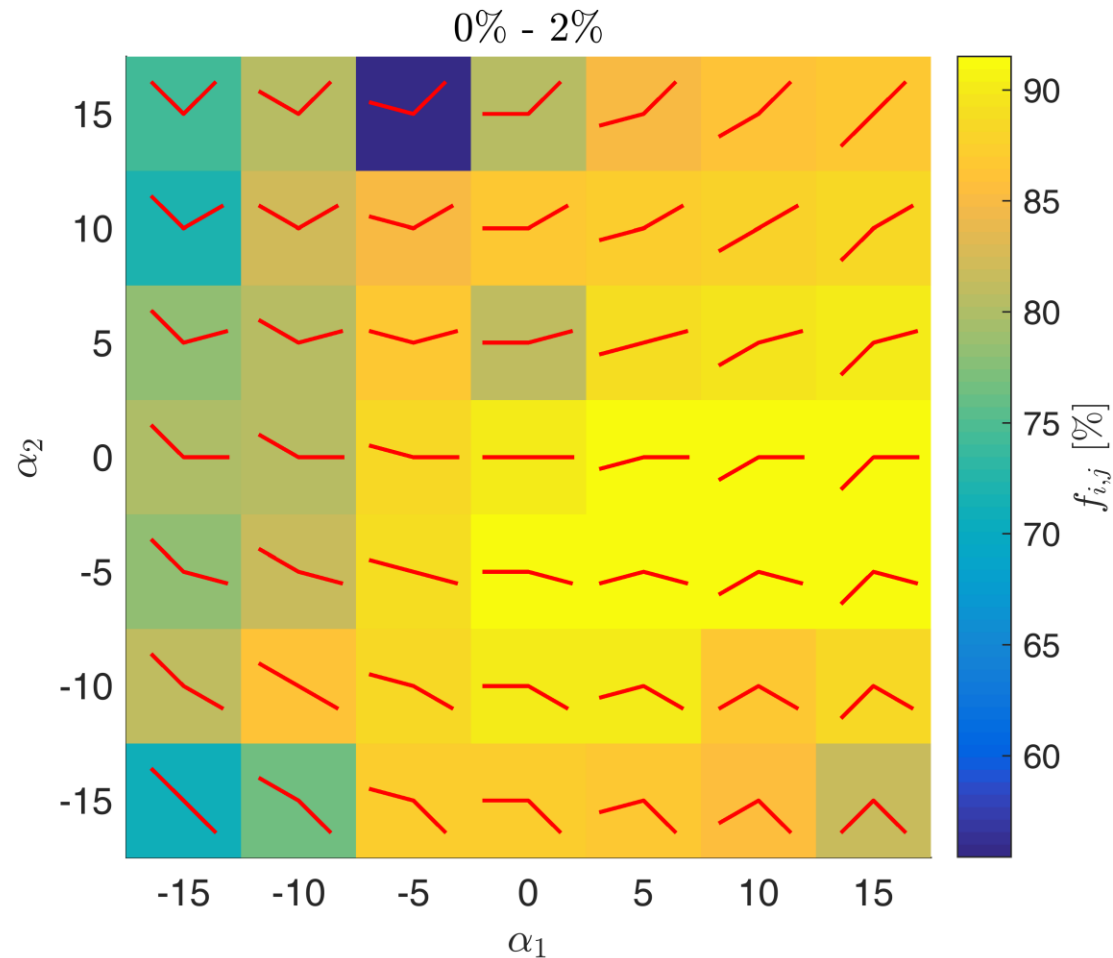
# Test simple model

- Isolate simple model error
- Test in an volume upstream

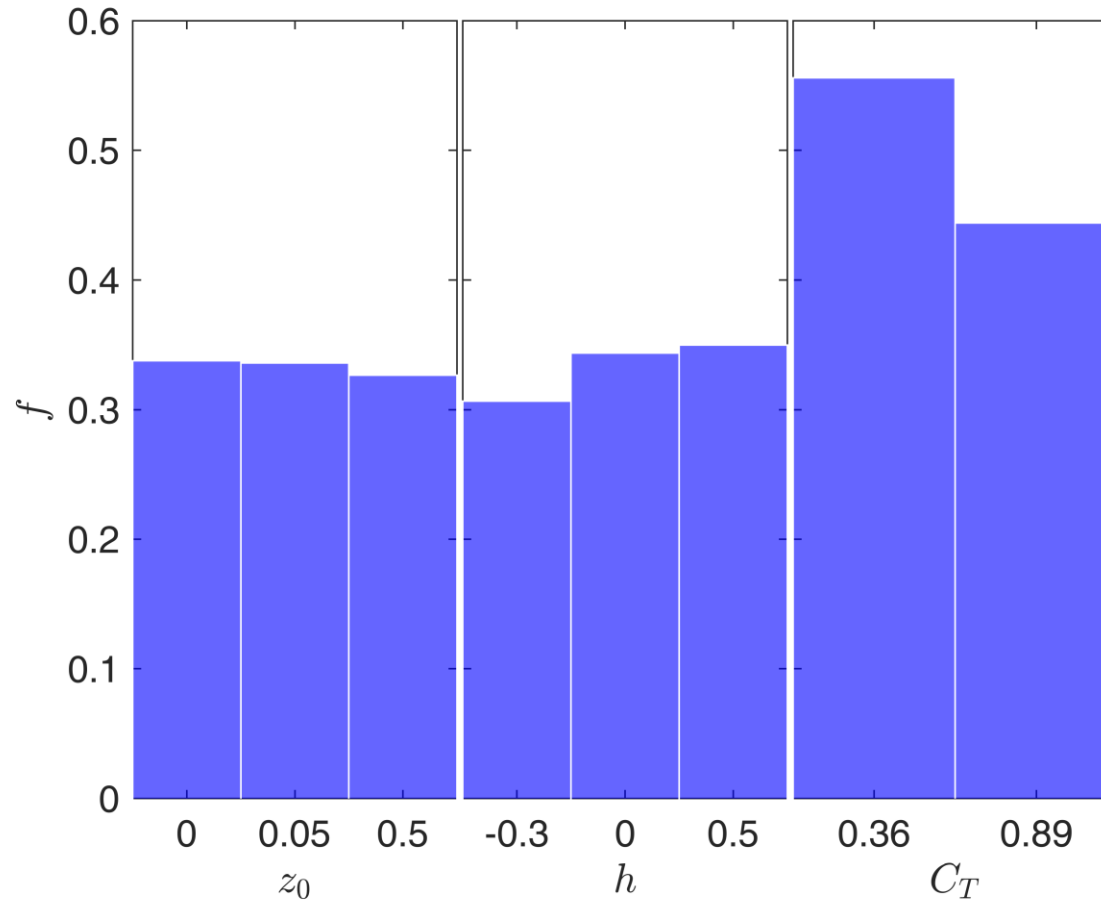


# Test simple model

- Only keep points that are below 2% error
- Group data over each hill shape



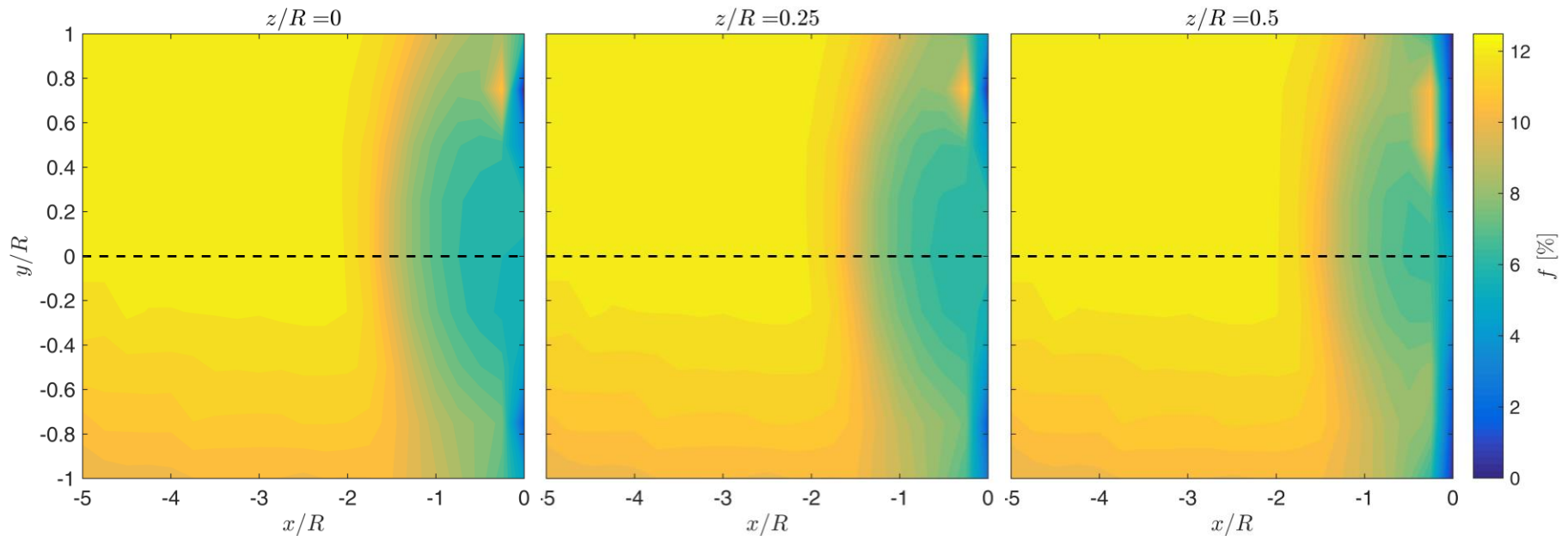
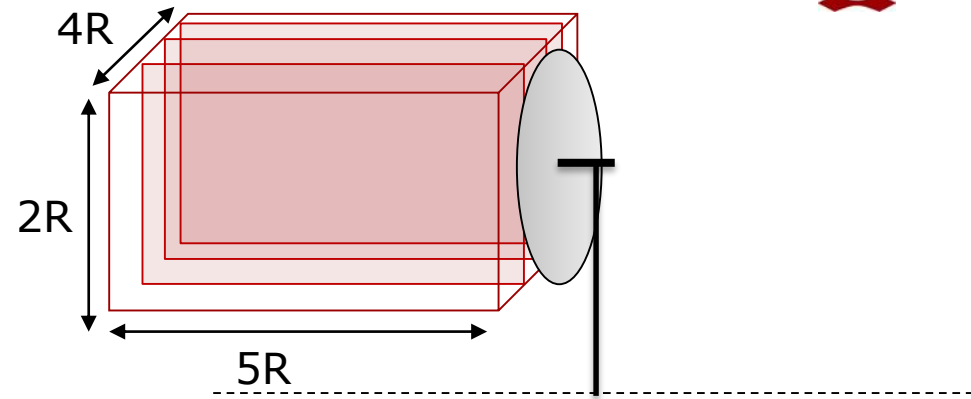
# Test simple model



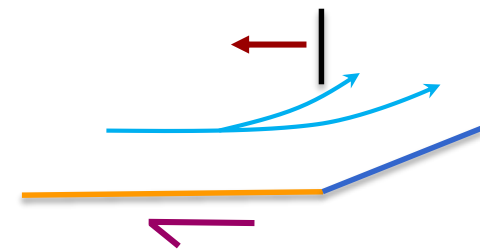
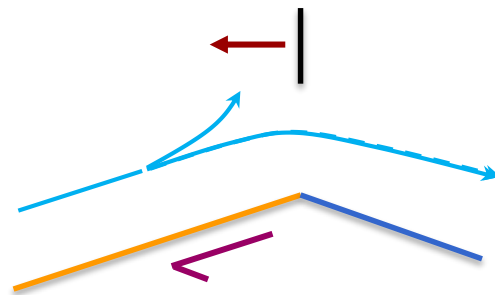
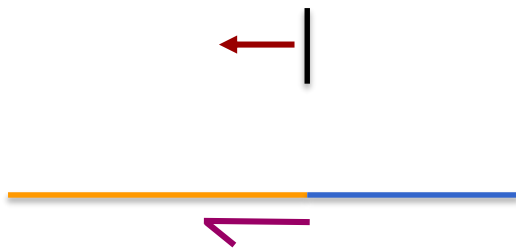
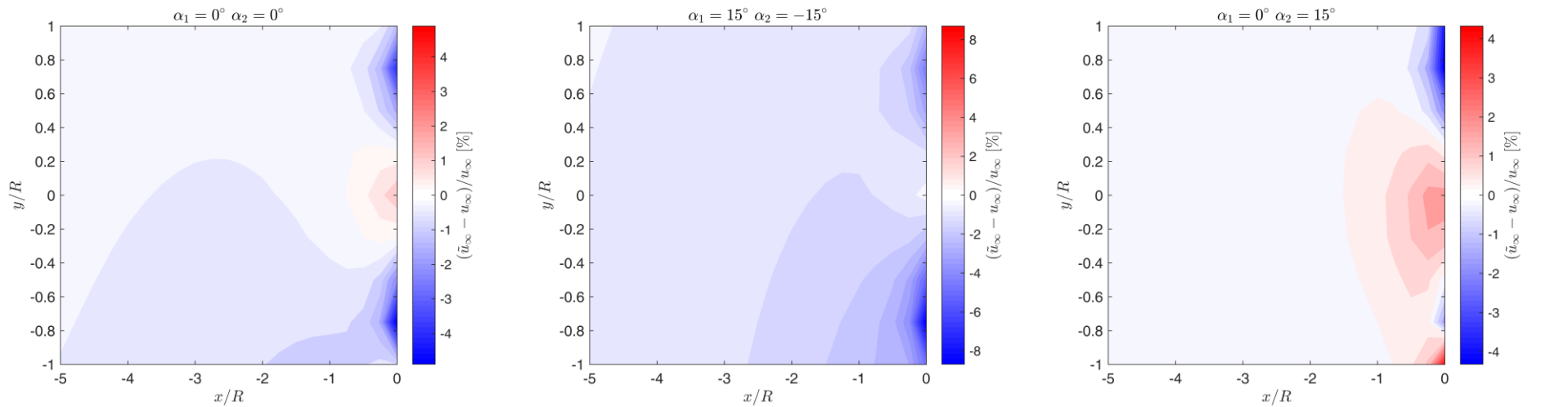


# Test simple model

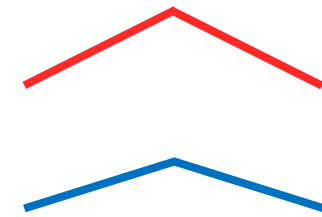
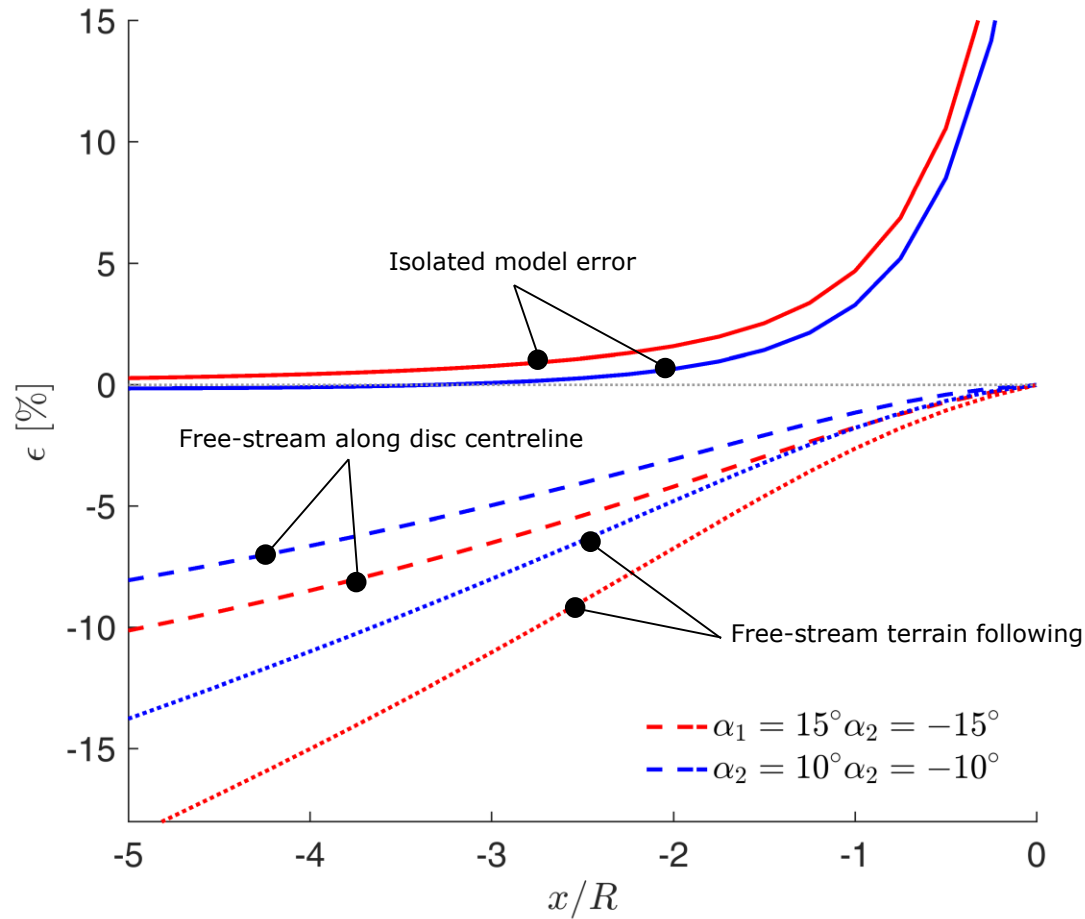
- Point density in x-y planes along constant depth



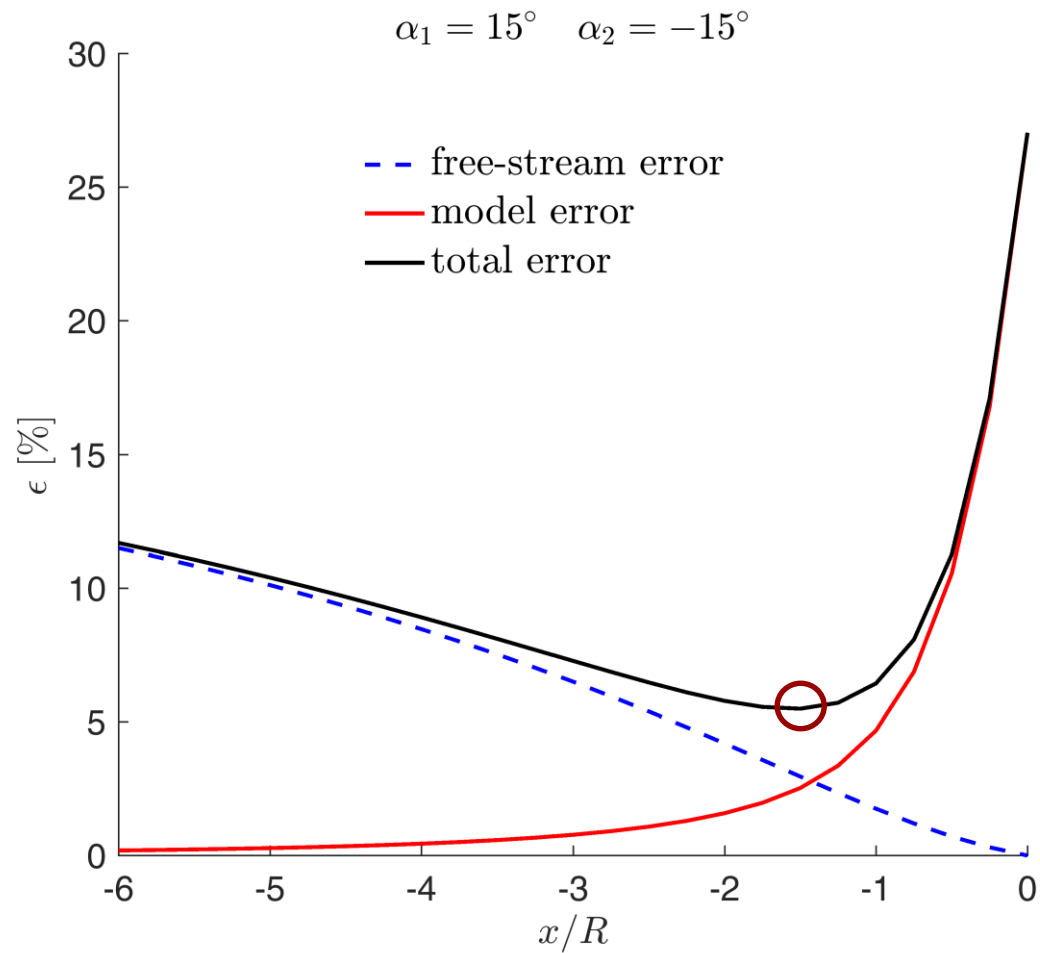
# Error source



# Error evolution along centreline

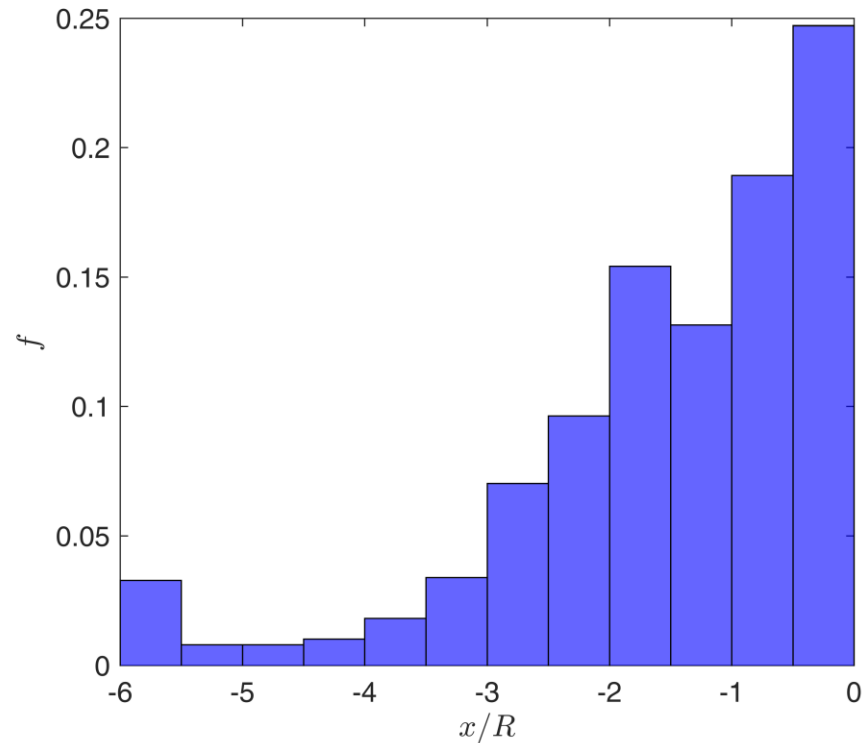


# Minimise error



# Minimum error location

- Minimum along centreline



# Conclusions

- Simple induction model works fine in moderate terrain
- Largest error from free-speed evolution
- Optimal measurement location lies close to rotor  $x < 3R$

# Outlook

## Measuring the free-stream

1. Measure relative close to turbine and use generic thrust curve
2. Use simple terrain model to predict  $V_\infty(x)$
3. Fit induction model +  $V_\infty(x)$

# Acknowledgements

# UniTTe.dk





**Thanks for your attention!**

