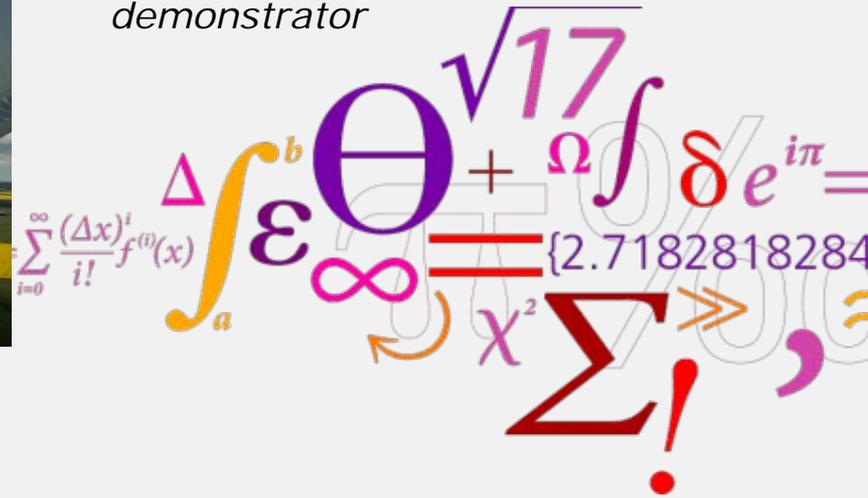


# Wind field reconstruction from nacelle-mounted profiling lidars for power performance



*ZephIR Dual-Mode*

*5-beam Avent demonstrator*



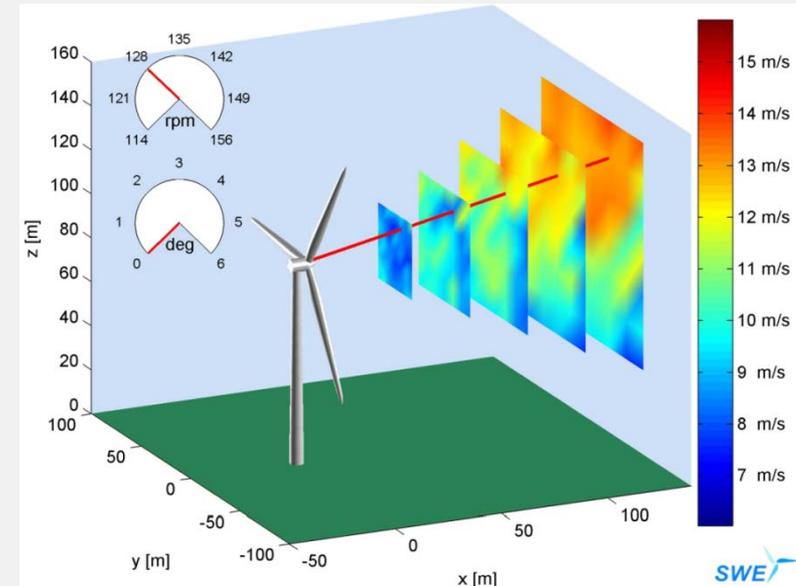
*A. Borraccino, DTU Wind Energy*

*with the support of  
D. Schlipf and F. Haizmann, SWE*

**DTU Wind Energy**  
Department of Wind Energy

# Nacelle-mounted lidars in WE: what for?

- Wind turbine control, incl. feed-forward ([Schlipf D.](#))
- Wakes measurements
- Yaw misalignment correction?



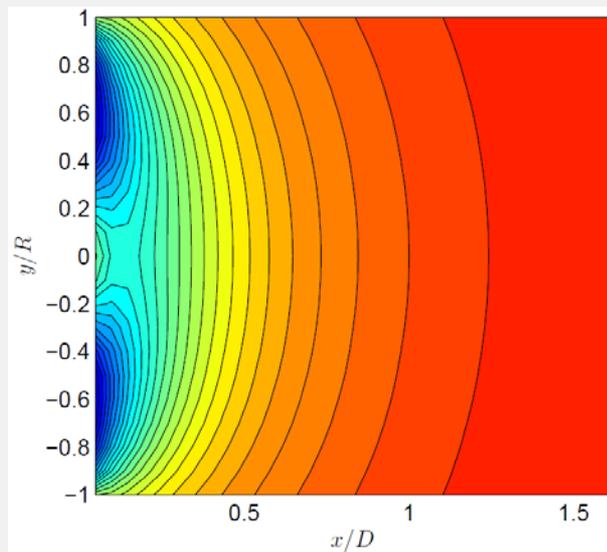
- **Power performance:** ([R. Wagner](#))  
to replace met. masts when
  - too expensive: offshore, complex sites
  - insufficient: wind spd at hub vs. REWS
  - free wind not measurable: decorrelation, no undisturbed sectors (offshore array, complex site, etc)

# Unified Turbine Testing (UniTTe)

- **UniTTe: Unified Turbine Testing**

- new methodology for power curve and loads assessment based on lidar near-flow measurements, i.e. close to the rotor, applicable in any type of terrain (radical change!)
- basis for future standards (e.g. IEC 614100-12-1)

**Numerical modelling of turbine inflow: induction 'transfer' function**



**Measurement campaigns: calibration + simple & complex terrain**

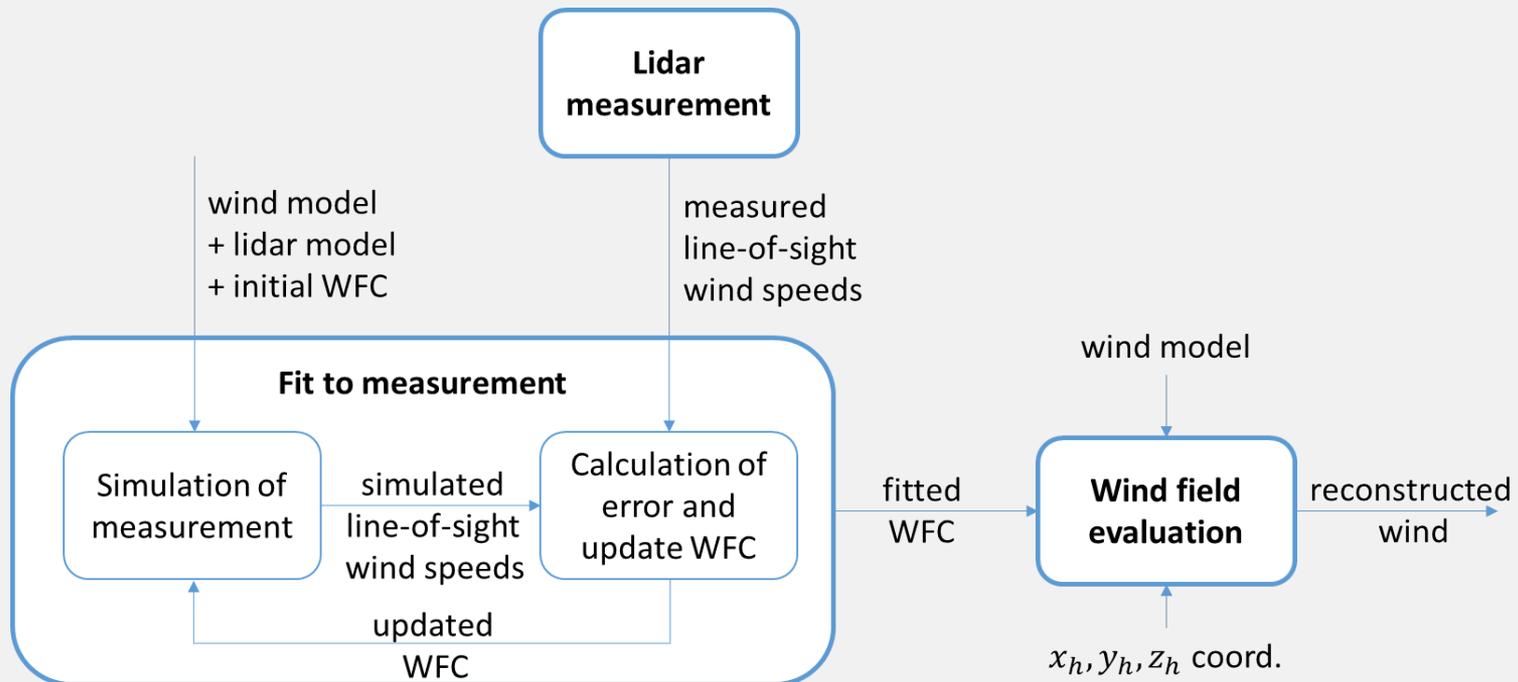


# Model-based wind field reconstruction

- **Doppler wind LiDaRs do not...**
  - ...measure wind speed, wind direction, shear, ...**
- see [Hardesty, 1987](#) (wonderful description of lidar principles)

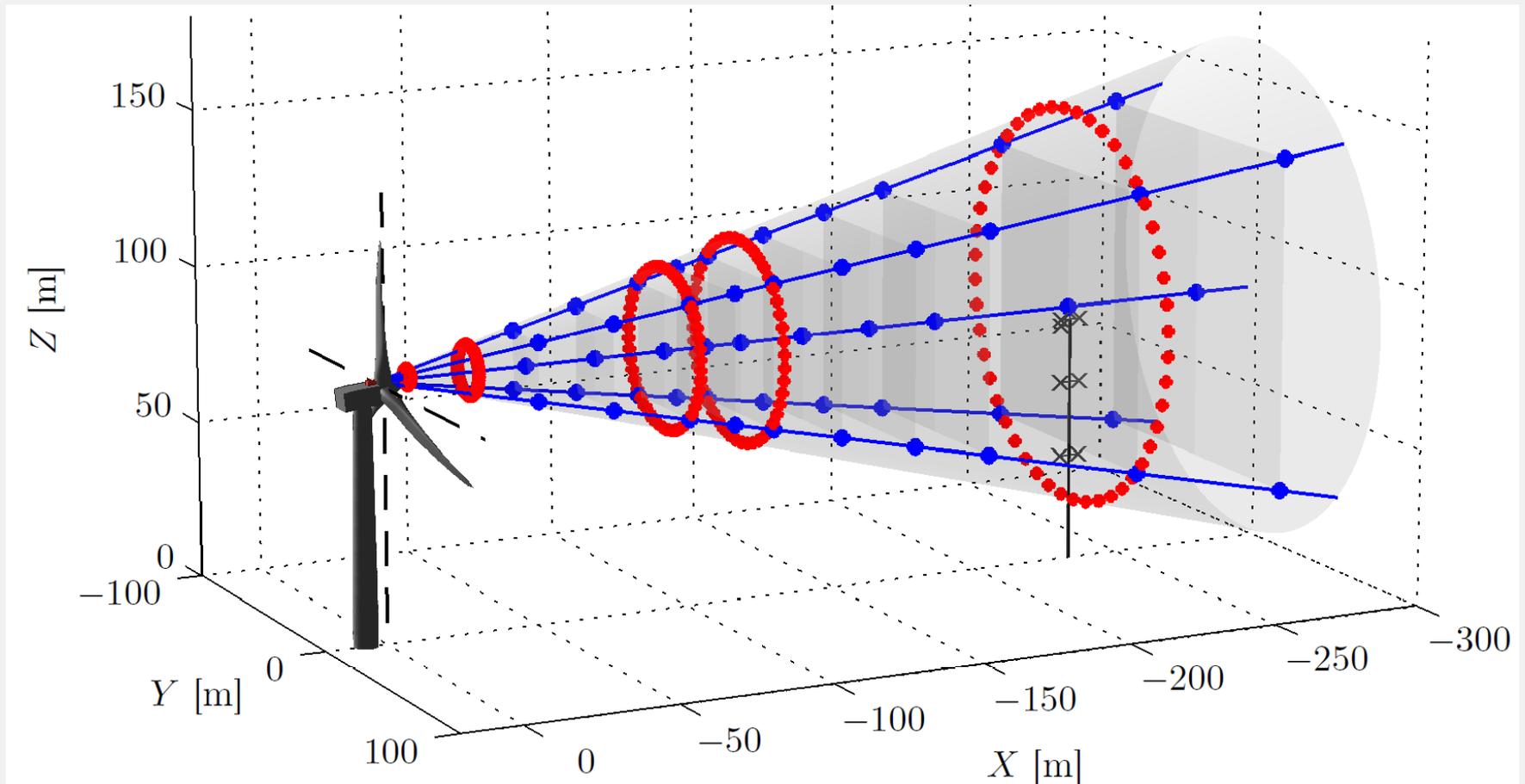
- **They:**

- only measure LOS velocities
- estimate/reconstruct wind field characteristics (WFC)



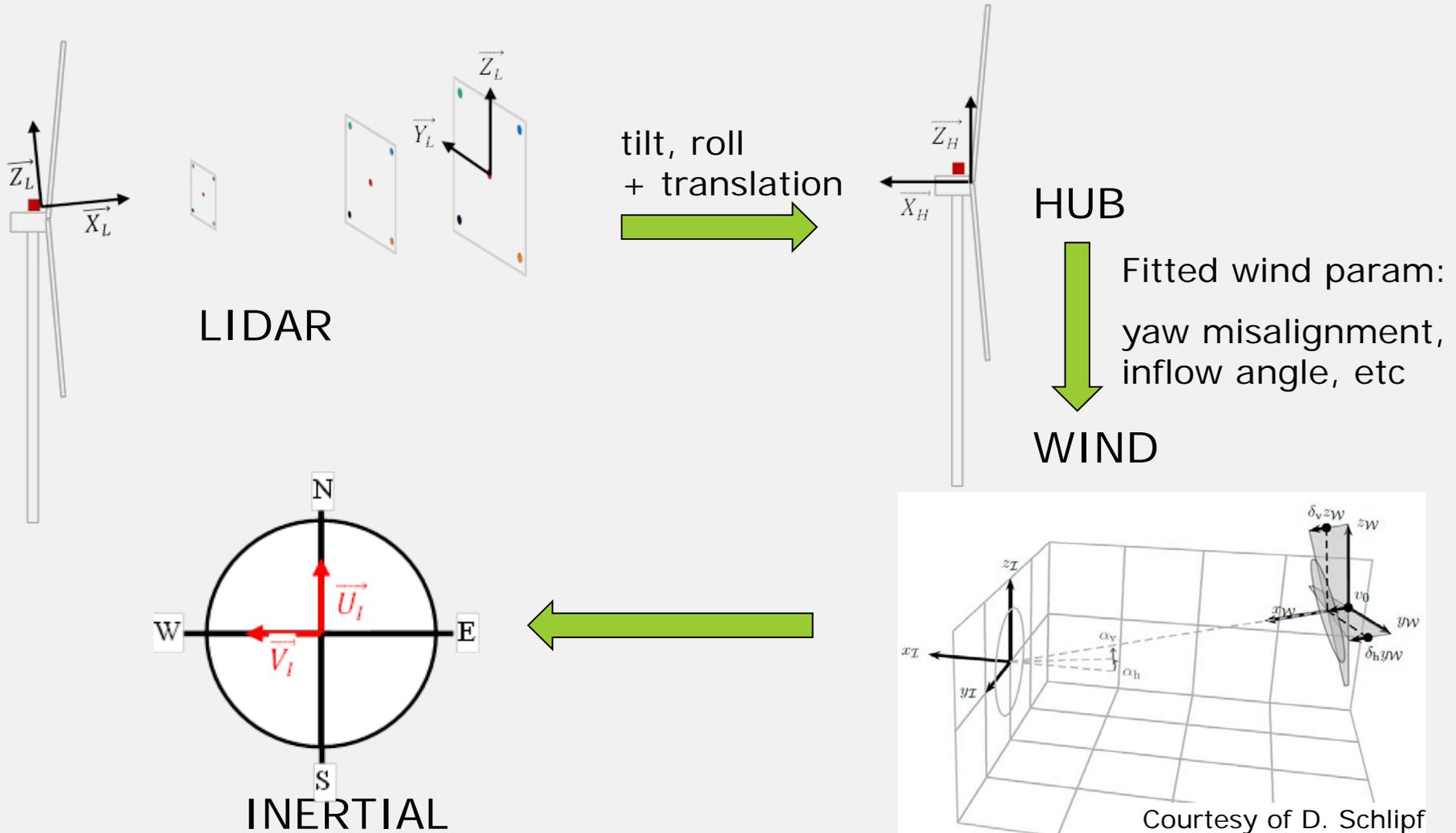
# Nørrekær Enge campaign (NKE), 7 months

- Two nacelle lidars:  
Avent 5-beam (5B) **in blue**, ZephIR Dual Mode (ZDM) **in red**
- IEC compliant mast + SCADA + full loads



# Model-based wind field reconstruction

## • Coordinate systems



# Model-based wind field reconstruction

- **Modelling the wind field**

- choose a wind model that fits the application & site characteristics
- the reconstruction should be performed either in the WIND coordinate systems or in the HUB

- **For power performance: static models**

- i.e. no time dependency
- use 10-min averages of:
  - LOS velocities
  - inclinometers readings
- use knowledge of the trajectory (opening angles, ranges config) and of lidar position

# Model-based wind field reconstruction

## • Wind models

Model	$U$	$V$	$W$	comment
Homogeneous 2D	$U_w = cst \leftrightarrow U_I = U$	$V_w = 0 \leftrightarrow V_I = V$	$W_w = 0 \leftrightarrow W_I = 0$	Does not depend on X, Y, Z
Homogeneous 3D	$U_w = cst \leftrightarrow U_I = U$	$V_w = 0 \leftrightarrow V_I = V$	$W_w = 0 \leftrightarrow W_I = W$	Does not depend on X, Y, Z

- Assumption of flow homogeneity
  - ➔ typically used by ground-based lidars (VAD, DBS) in flat terrain
  - ➔ not making much sense for lidars in nacelle mode because of variations with heights a.g.l. (shear, veer, etc.)

# Model-based wind field reconstruction

## • Wind models

Model	$U$	$V$	$W$	comment
Homogeneous 2D	$U_w = cst \leftrightarrow U_I = U$	$V_w = 0 \leftrightarrow V_I = V$	$W_w = 0 \leftrightarrow W_I = 0$	Does not depend on $X, Y, Z$
Homogeneous 3D	$U_w = cst \leftrightarrow U_I = U$	$V_w = 0 \leftrightarrow V_I = V$	$W_w = 0 \leftrightarrow W_I = W$	Does not depend on $X, Y, Z$
Inhomogeneous 2D + linear V shear	$U_w = v_0 + \delta_V \cdot (z_w - z_{hub})$ $\leftrightarrow U_I = f(z)$	$V_w = 0 \leftrightarrow V_I = V$	$W_w = 0 \leftrightarrow W_I = 0$	Yaw misalignment $\alpha_H = cst$
Inhomogeneous 2D + linear V shear + linear V veer	$U_w = v_0 + \delta_V \cdot (z_w - z_{hub})$ $\leftrightarrow U_I = f(z)$	$V_w = 0 \leftrightarrow V_I = f(z)$	$W_w = 0 \leftrightarrow W_I = 0$	Yaw misalignment $\alpha_H = f(z)$
<b>Inhomogeneous 2D + power law shear</b>	$U_w = v_0 (z_w / z_{hub})^{\alpha_{exp}}$ $\leftrightarrow U_I = f(z)$	$V_w = 0 \leftrightarrow V_I = V$	$W_w = 0 \leftrightarrow W_I = 0$	<b>Yaw misalignment</b> $\alpha_H = cst$

↳ fitted wind characteristics are:

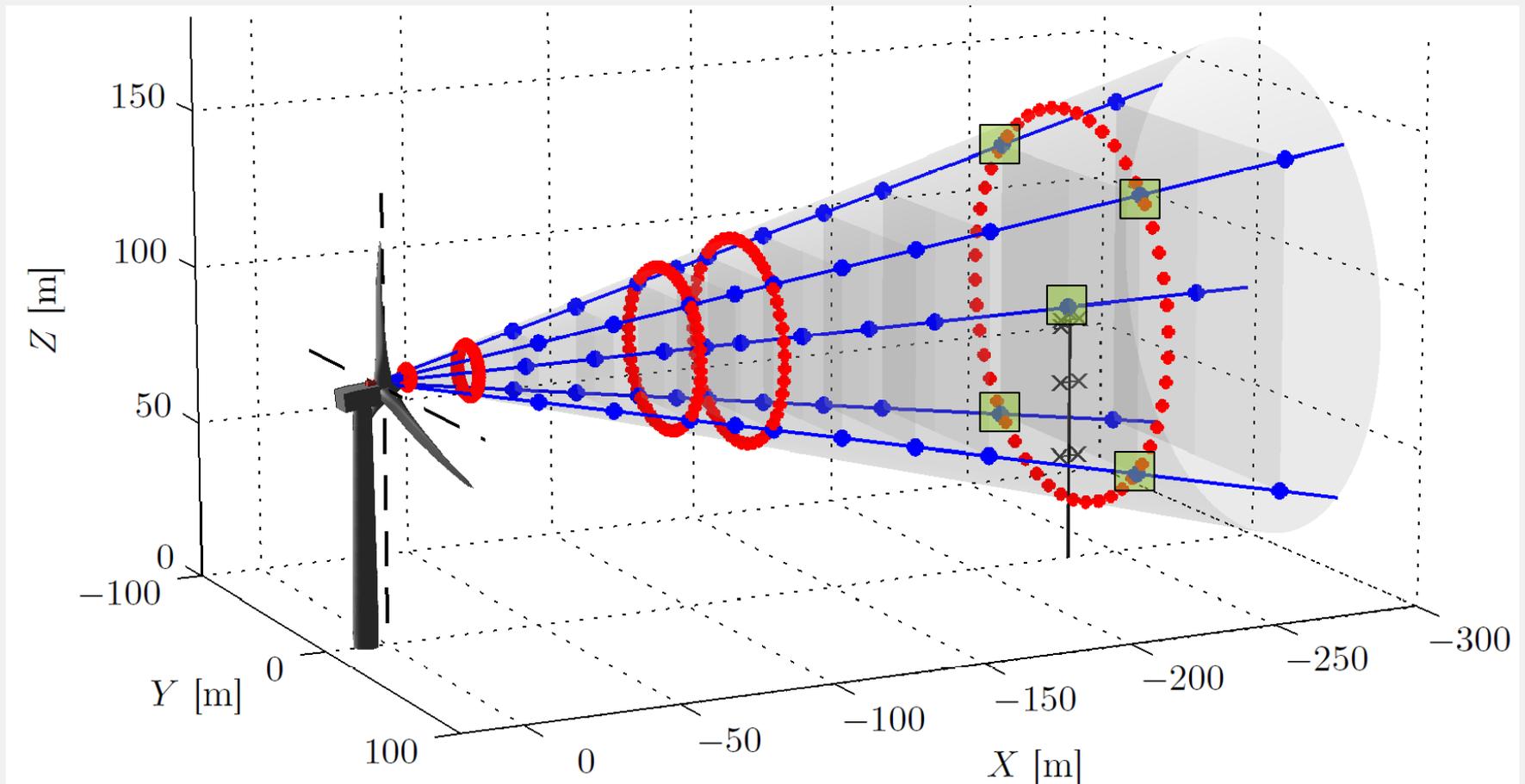
- HWS  $v_0$
- yaw misalignment  $\alpha_H$  (relative wind dir)
- shear exponent  $\alpha_{exp}$

# Results: Inhomogeneous 2D with shear exp

5B: use all 5 pts

ZDM: use 4 pts in square

Free sector  $[110; 219]^\circ$  ; @2.5  $D_{rot}$  ; HWS estimated @hub

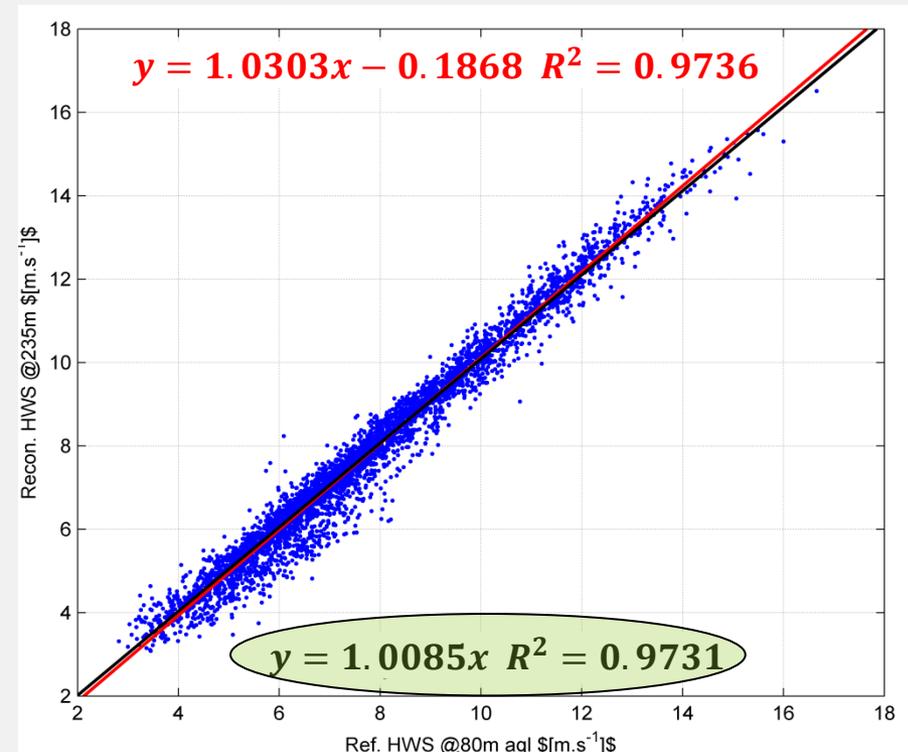
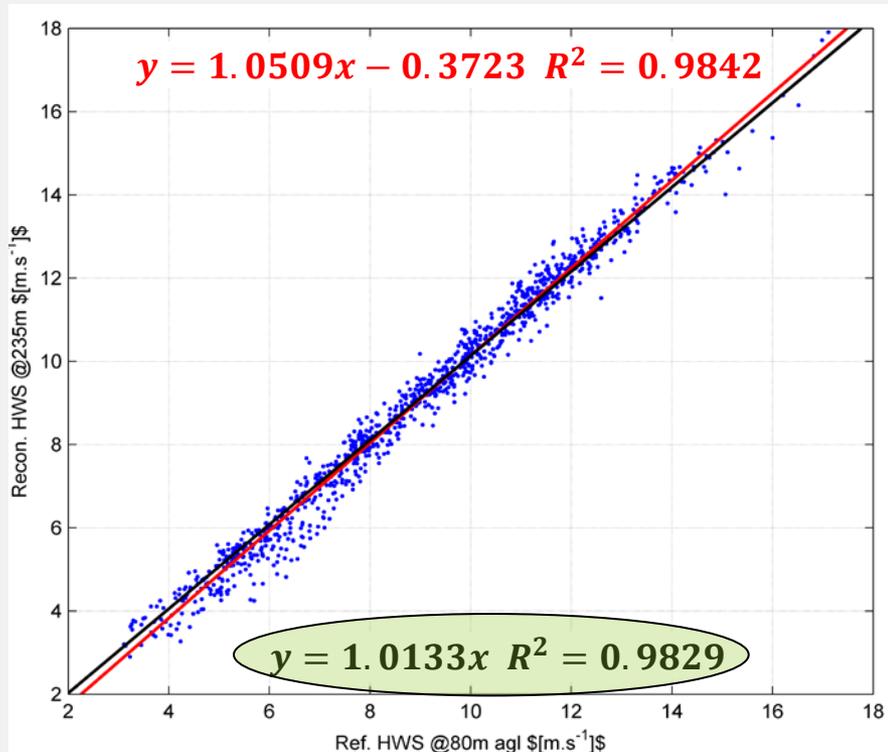


# Results: Inhomogeneous 2D with shear exp

5B: use all 5 pts

ZDM: use 4 pts in square

Free sector  $[110; 219]^\circ$  ; @2.5  $D_{rot}$  ; HWS estimated @hub

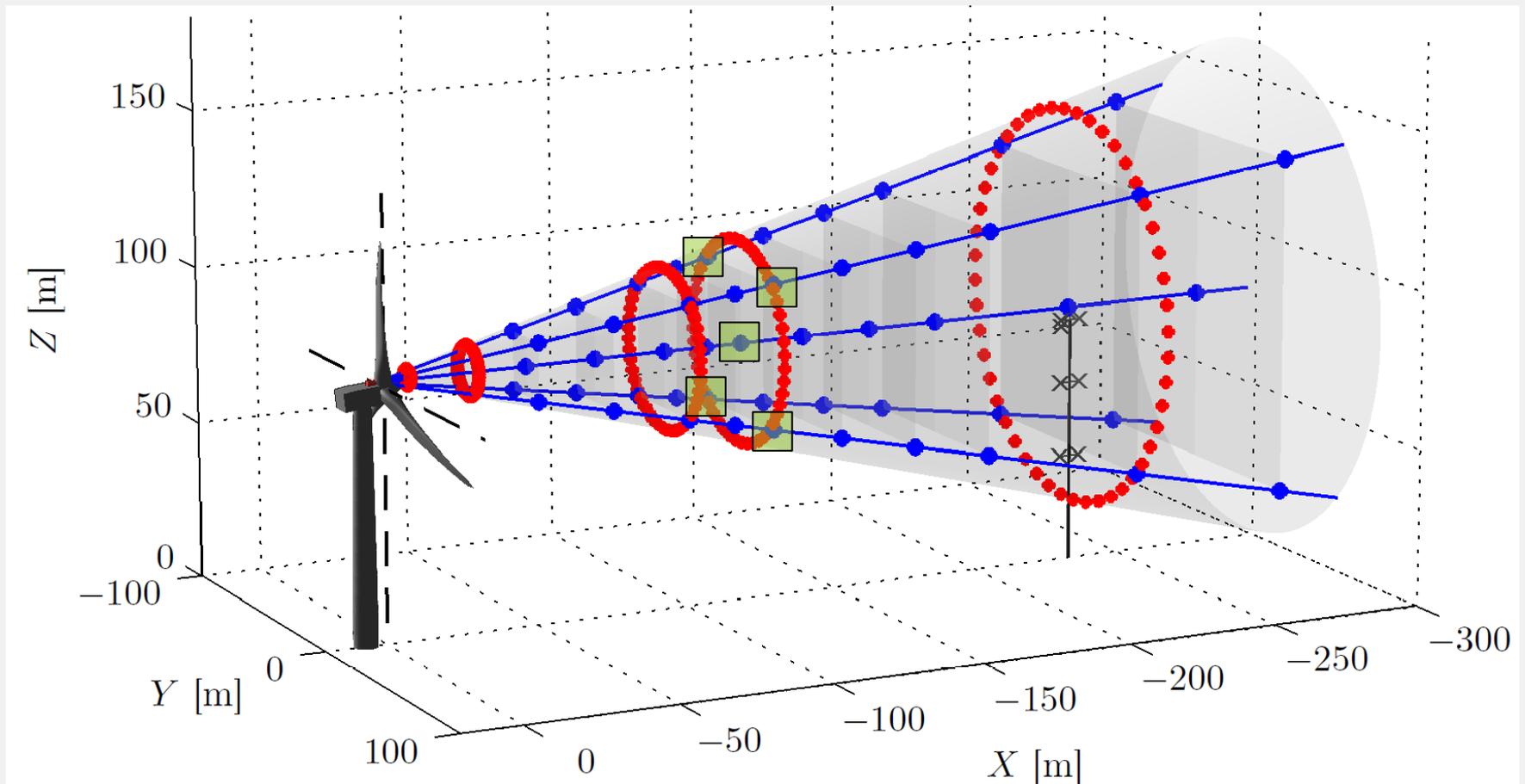


# Results: Inhomogeneous 2D with shear exp

5B: use all 5 pts

ZDM: use 4 pts in square

Free sector  $[110; 219]^\circ$  ; @1.0  $D_{rot}$  ; HWS estimated @hub



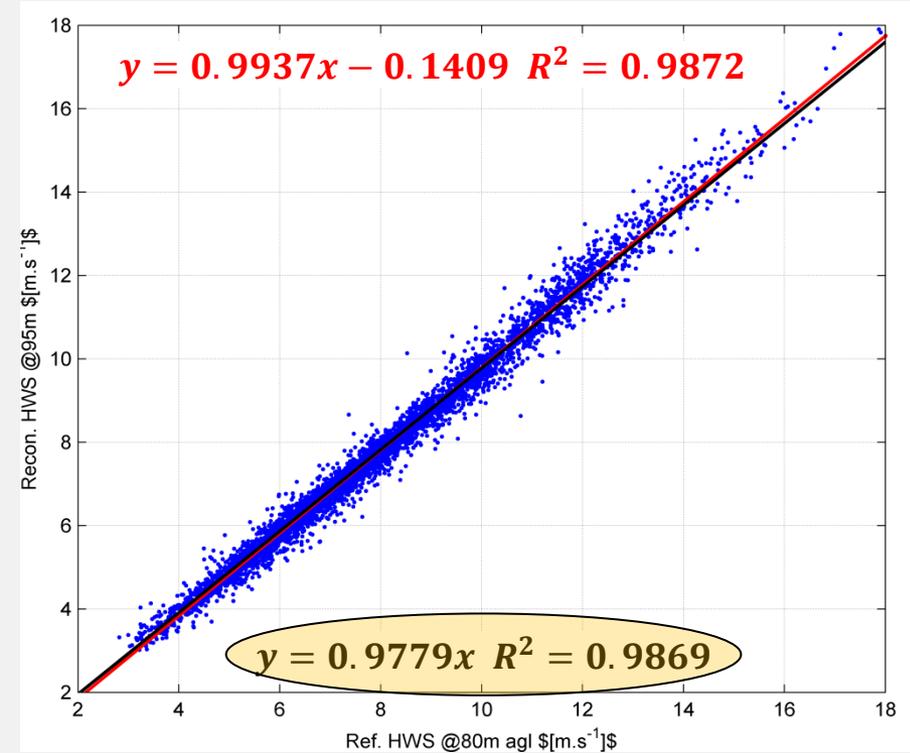
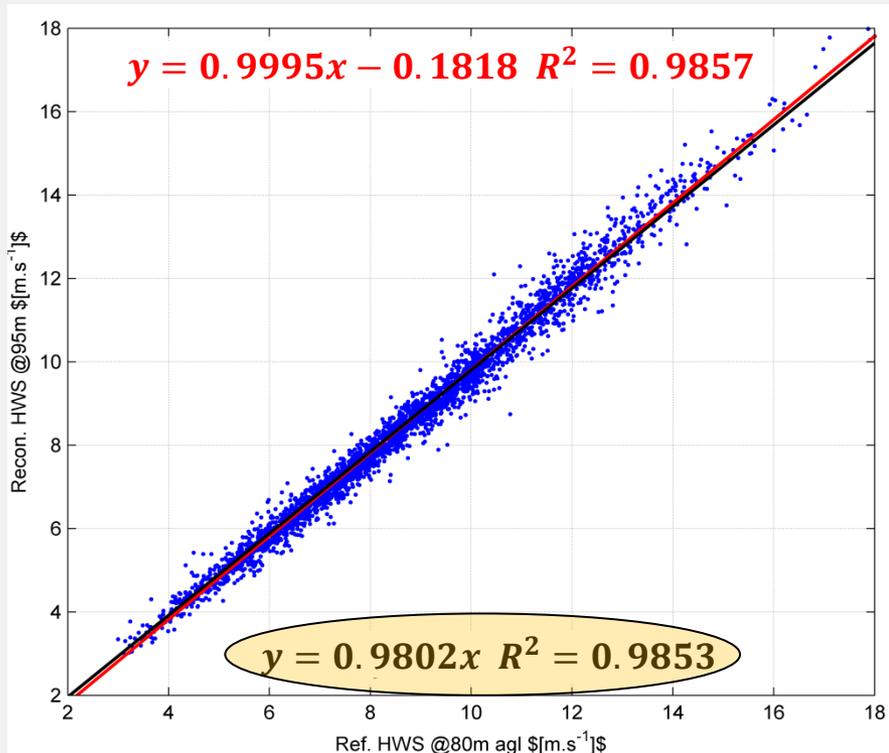
# Results: Inhomogeneous 2D with shear exp



5B: use all 5 pts

ZDM: use 4 pts in square

Free sector  $[110; 219]^\circ$  ; @1.0  $D_{rot}$  ; HWS estimated @hub



less scatter, wind speed deficit of ~2% → can we correct this?

# A simple induction model

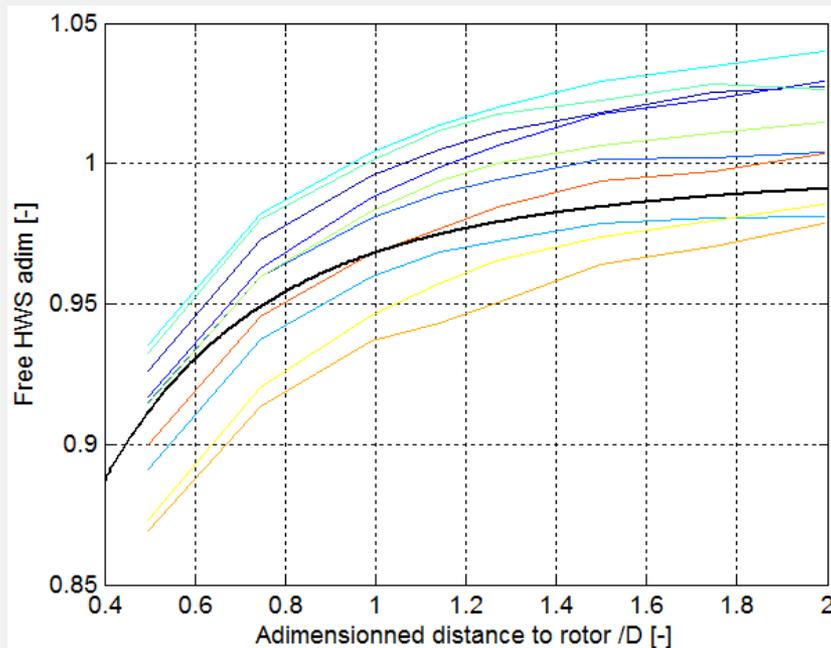
- **Derived from the Biot-Savart law**

- see [The upstream flow of a wind turbine: blockage effect](#)

- two parameters: induction factor  $a$ , free wind speed  $U_\infty$

$$\frac{U}{U_\infty} = 1 - a \left( 1 + \frac{\xi}{\sqrt{1+\xi^2}} \right), \text{ with } \xi = \frac{x_W}{R_{rot}}$$

- **What does the induction looks like in NKE?**



Black: theoretical,  $a = 0.3$

Colored lines: different 10min periods

→ Fitting  $a$  and  $U_\infty$  should be possible

# Model-based wind field reconstruction

## • Wind models

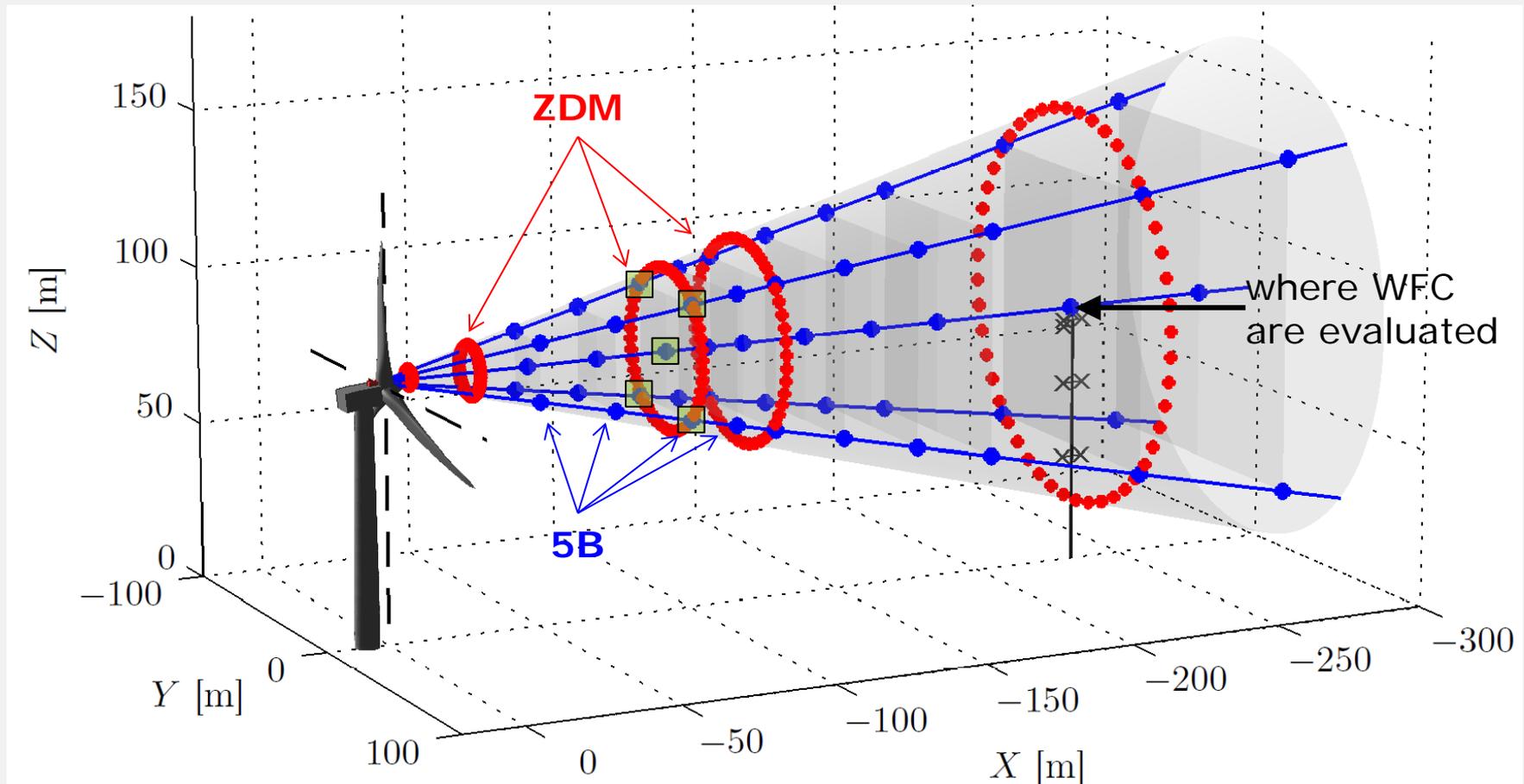
Model name	$U$	$V$	$W$	comment
Homogeneous 2D	$U_w = cst \leftrightarrow U_I = U$	$V_w = 0 \leftrightarrow V_I = V$	$W_w = 0 \leftrightarrow W_I = 0$	Does not depend on X, Y, Z
Homogeneous 3D	$U_w = cst \leftrightarrow U_I = U$	$V_w = 0 \leftrightarrow V_I = V$	$W_w = 0 \leftrightarrow W_I = W$	Does not depend on X, Y, Z
Inhomogeneous 2D + linear V shear	$U_w = v_0 + \delta_V \cdot (z_w - z_{hub})$ $\leftrightarrow U_I = f(z)$	$V_w = 0 \leftrightarrow V_I = V$	$W_w = 0 \leftrightarrow W_I = 0$	Yaw misalignment $\alpha_H = cst$
Inhomogeneous 2D + linear V shear + linear V veer	$U_w = v_0 + \delta_V \cdot (z_w - z_{hub})$ $\leftrightarrow U_I = f(z)$	$V_w = 0 \leftrightarrow V_I = f(z)$	$W_w = 0 \leftrightarrow W_I = 0$	Yaw misalignment $\alpha_H = f(z)$
Inhomogeneous 2D + power law shear	$U_w = v_0 (z_w / z_{hub})^{\alpha_{exp}}$ $\leftrightarrow U_I = f(z)$	$V_w = 0 \leftrightarrow V_I = V$	$W_w = 0 \leftrightarrow W_I = 0$	Yaw misalignment $\alpha_H = cst$
<b>Inhomogeneous 2D + power law shear + induction model</b>	$U_w = f(x, z)$ $\leftrightarrow U_I = f(x, z)$	$V_w = 0$ $\leftrightarrow V_I = f(x, z)$	$W_w = 0 \leftrightarrow W_I = 0$	<b>1D Biot-Savard for induction fct</b>


 fitted wind characteristics are: free stream HWS  $U_\infty$ , yaw misalignment  $\alpha_H$ , shear exponent  $\alpha_{exp}$ , induction factor  $a$ .

# Results: 'free' wind speed based on near flow measurements

5B: use all 5 pts  
+ 4 dist. (0.5 to 1.1D)

ZDM: use 4 pts in square  
+ 3 dist. (0.3 to 1.2D)

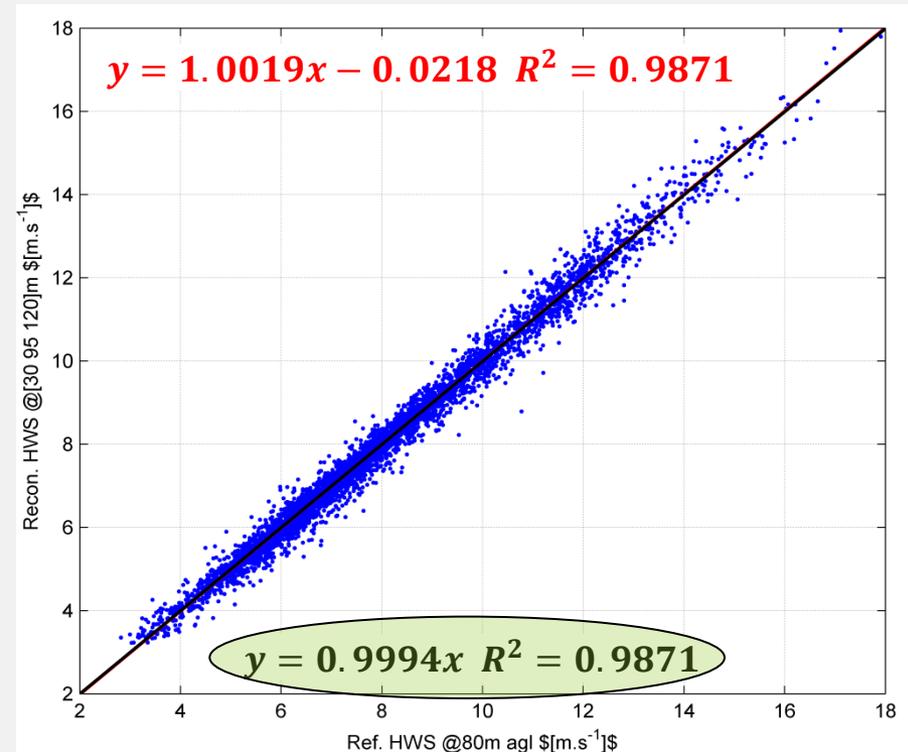
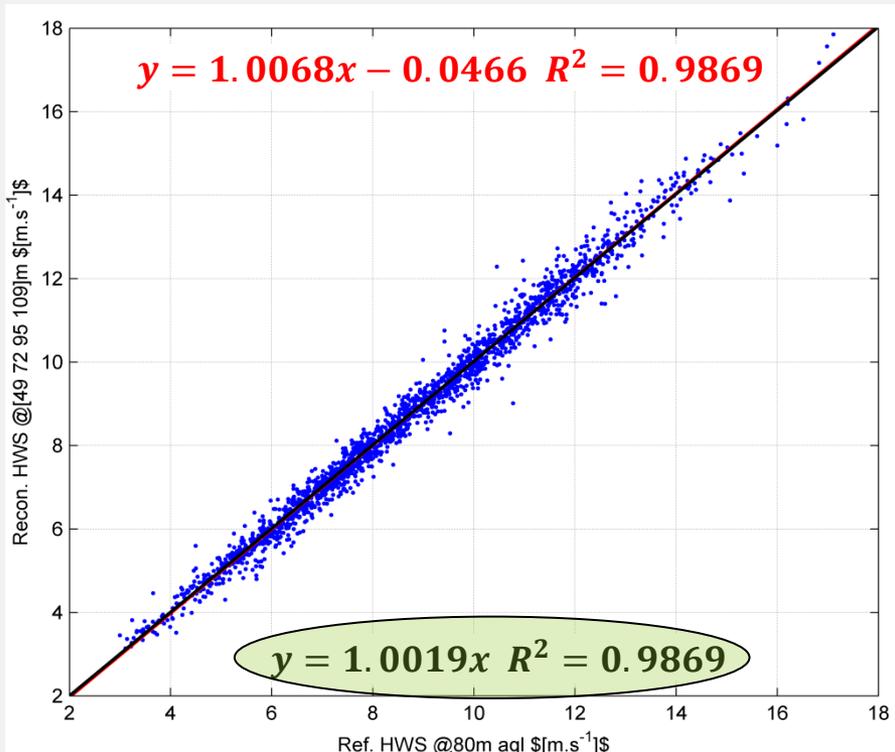


# Results: 'free' wind speed based on near flow measurements

5B: use all 5 pts  
+ 4 dist. (0.5 to 1.1D)

ZDM: use 4 pts in square  
+ 3 dist. (0.3 to 1.2D)

Free sector  $[110; 219]^\circ$  ; HWS estimated @  $H_{\text{hub}}$  &  $2.5 D_{\text{rot}}$

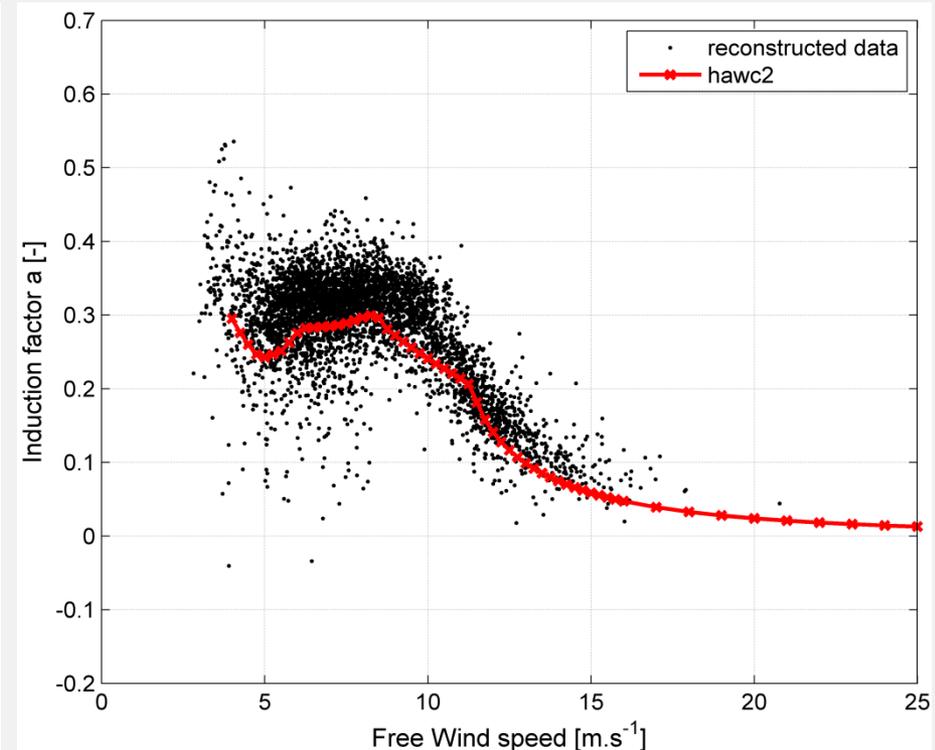
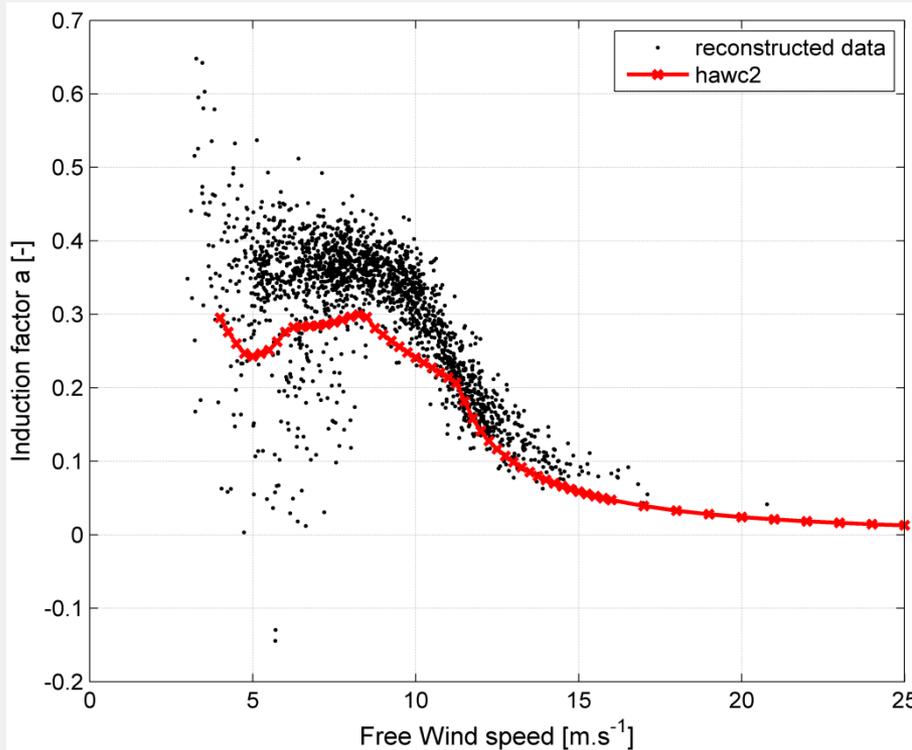


# Induction factor?

Estimated as part of the outputs of the induction model

➔ can even be considered a lidar-estimation of thrust coeff.

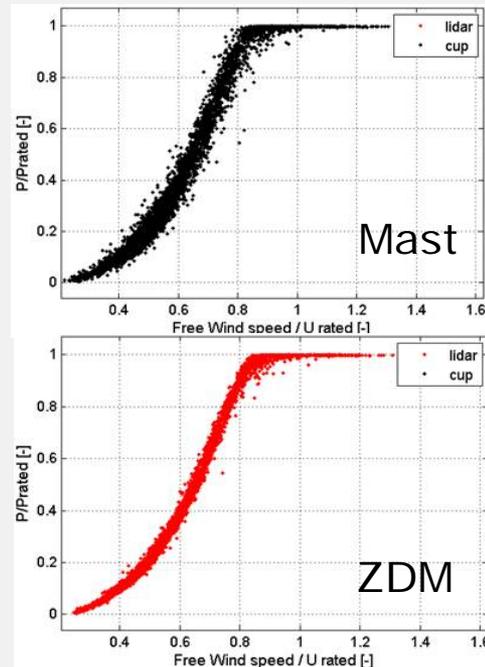
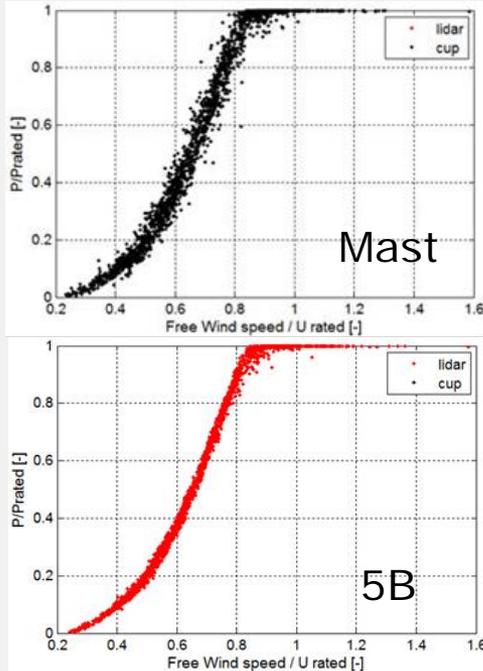
Induction factor vs. free stream wind speed  
(5B left, ZDM right)



# Conclusions

- Model-based wind field reconstruction provides estimations of wind characteristics comparable with classic anemometry
- Integrating an induction model is possible (same for wakes?)
- Combined with near-flow measurements, the method allows robust estimation of 'free stream' wind
- **Questions & further work:**
  1. How to adapt the models to complex terrain? Same?
  2. Should the induction function be made 2-dimensional?
  3. Quantify uncertainties on wind characteristics estimates using calibrated LOS velocity measurements
- Preliminary power curves show reduced scatter and high accuracy

# Thanks for your attention!



More info:

- website [www.unitte.dk](http://www.unitte.dk)
- contact [borr@dtu.dk](mailto:borr@dtu.dk)

# Acknowledgements



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Thanks to David Schlipf, Florian Haizmann and all SWE for the good collaboration that made this work possible.